

IHP 2006

Testing the Equivalence Principle in Space

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Stanford University

IHP 2006

Experimental Tests of



© Alan Bean, courtesy Greenwich Workshop Inc

Space provides unique opportunities to advance fundamental physics enabling new experiments of unprecedented precision impossible to perform on the ground

– these experiments cover the range of Condensed matter, Atomic physics, Particle Physics And Gravitational physics

8 means by which space enables new experiments

- | | |
|------------------------------|----------------------------------------------------------------------------------------------------------------------------------------------------------------------------|
| <i>Above the atmosphere.</i> | Removes difficulties including: optical tracking – GP-B
Particle annihilation in antimatter searches like AMS
Absorption of radiation in γ ray missions GLAST |
| <i>Remote benchmarks.</i> | Retroreflectors on the Moon, radar transponders on Mars, Cassini relativity experiment |
| <i>Large distances.</i> | A gravitational antenna with masses 5×10^6 km apart (LISA) enables new frequency range over ground antennas |
| <i>Reduced gravity.</i> | 'Microgravity' (10^{-4} to 10^{-6} g levels) enables new laser cooling and condensed matter physics experiments; Helium λ piont and CHeX, ACES |

8 means by which space enables new experiments, cont.

Isolation from seismic and gravitational noise.

Drag-free operation for GP-B, MicroSCOPE, STEP and LISA

Varying ϕ

Some physical effects (e.g. the Einstein redshift) vary with the gravitational *potential*

Varying g .

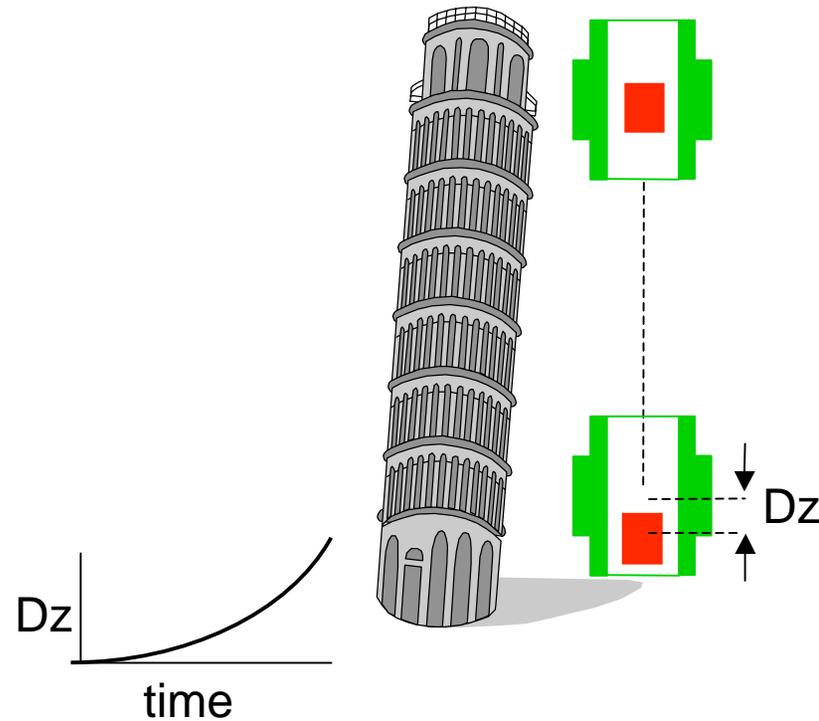
Other effects (equivalence principle tests) vary with the magnitude or direction of the gravitational *acceleration*

Separation of effects.

Choosing a particular orbit can separate effects that would be hopelessly entangled in any corresponding ground-based experiments: Gravity Probe B

Testing the Equivalence Principle

Newton's Mystery $\left\{ \begin{array}{l} F = ma \\ F = GMm/r^2 \end{array} \right.$ mass - the receptacle of inertia
mass - the source of gravitation

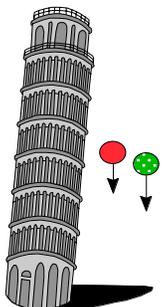
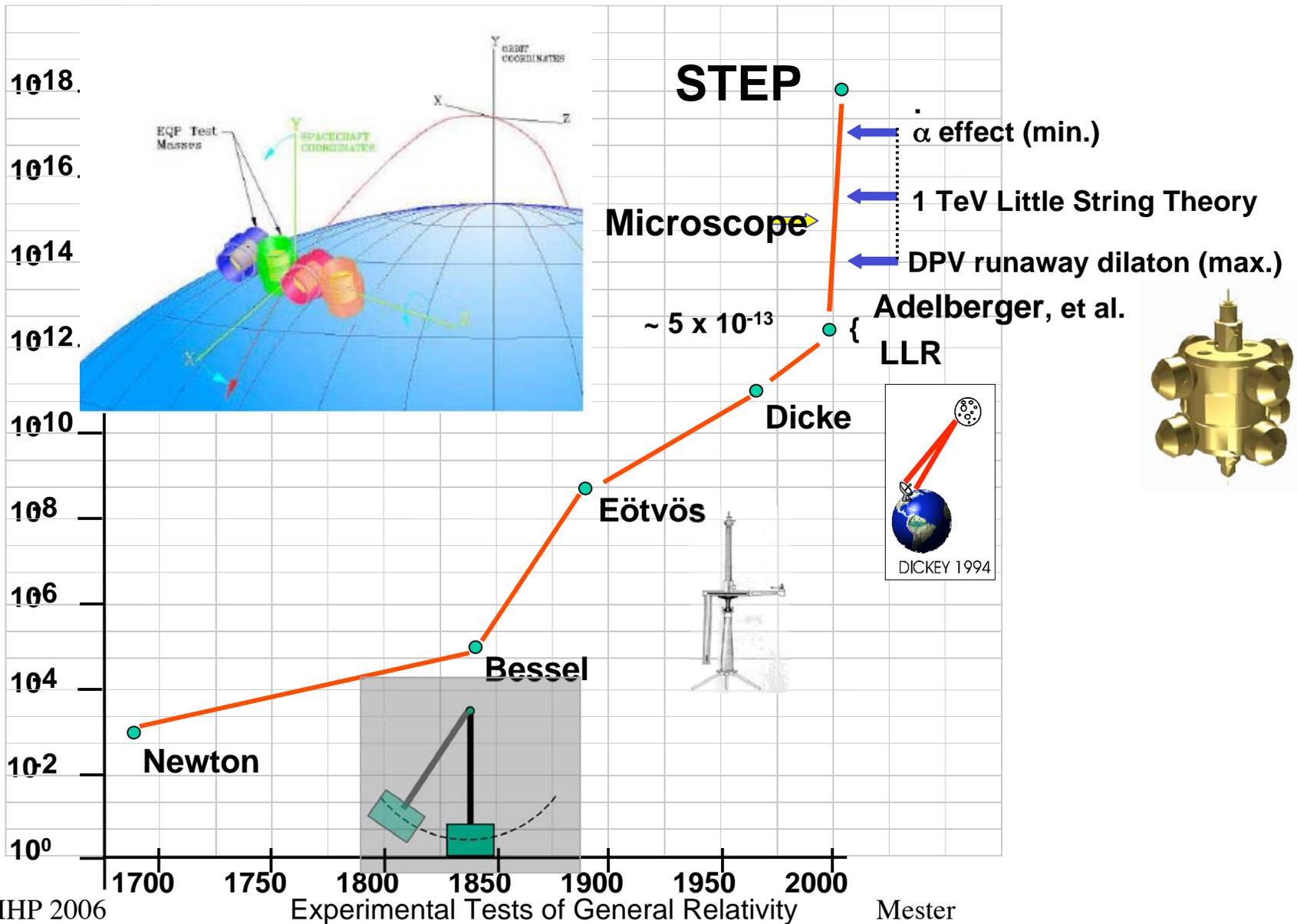


WEP \Rightarrow Universality of Free Fall

EP Is a postulate of General Relativity, its not explained by it.

Space > 5 Orders of Magnitude Leap

Goal: 1 part in 10^{15} - 10^{18}



MicroSCOPE and STEP

Two specific space based Equivalence Principle (EP) experiments have undergone significant study.

MicroSCOPE, a French led microsatellite mission planned for launch in 2009 or 2010, and

STEP, a US-European Collaboration that recently completed a SMEX (Small Explorer Phase A study.

Both missions take advantage of the ultra quiet and stable platform created by drag free control, reducing the leading seismic disturbance limitations of ground based experiments.

Proposed Equivalence Principle Tests in Space

<i>Proposal</i>	<i>Institution</i>	<i>Accuracy Goal</i>
<i>SEE</i> Satellite Energy Exchange	U. Tennessee	Unspecified
<i>Microscope</i> MICRO-Sat à traînée Compensée pour l'Observation du PE	ONERA, OCA, CNES, ESA	1×10^{-15}
<i>Equivalence</i> Balloon Drop Test of EP	Harvard SAO, IFSI Rome	1×10^{-15}
<i>GG</i> Galileo Galilei	Università di Pisa	1×10^{-17}
<i>STEP</i> Satellite Test of EP	Stanford, NASA MSFC European Collaboration	1×10^{-18}

STEP & Microscope History

- **Concept Developed, (Chapmen, Hansen, Worden, Everitt) 1970-71**
- **STEP, QuickSTEP, MiniSTEP and ESA Phase A Studies**
 - Supported under NASA Code U, \$23M investment, 1980s to 2002
 - Worden/Everitt propose STEP to ESA AO, 11/89
 - Awarded flight assessment study, Euro team formed, 1990 (only Fund Phys Mission)
 - Awarded ESA M2 Phase A study, 1991 - not selected for flight
 - Proposed by European team for M3, Awarded Phase A study

• **GeoSTEP and GG Proposed as French & Italian led missions, resp**

• **GeoSTEP => Microscope**

- Selected as Third MicroSat of CNES Myriade Series, 2000
- Instrument PDR 2006
- Flight Scheduled 2009-2010

• **STEP completed NASA OBPR SCR/RDR w/Euro team, 1999**

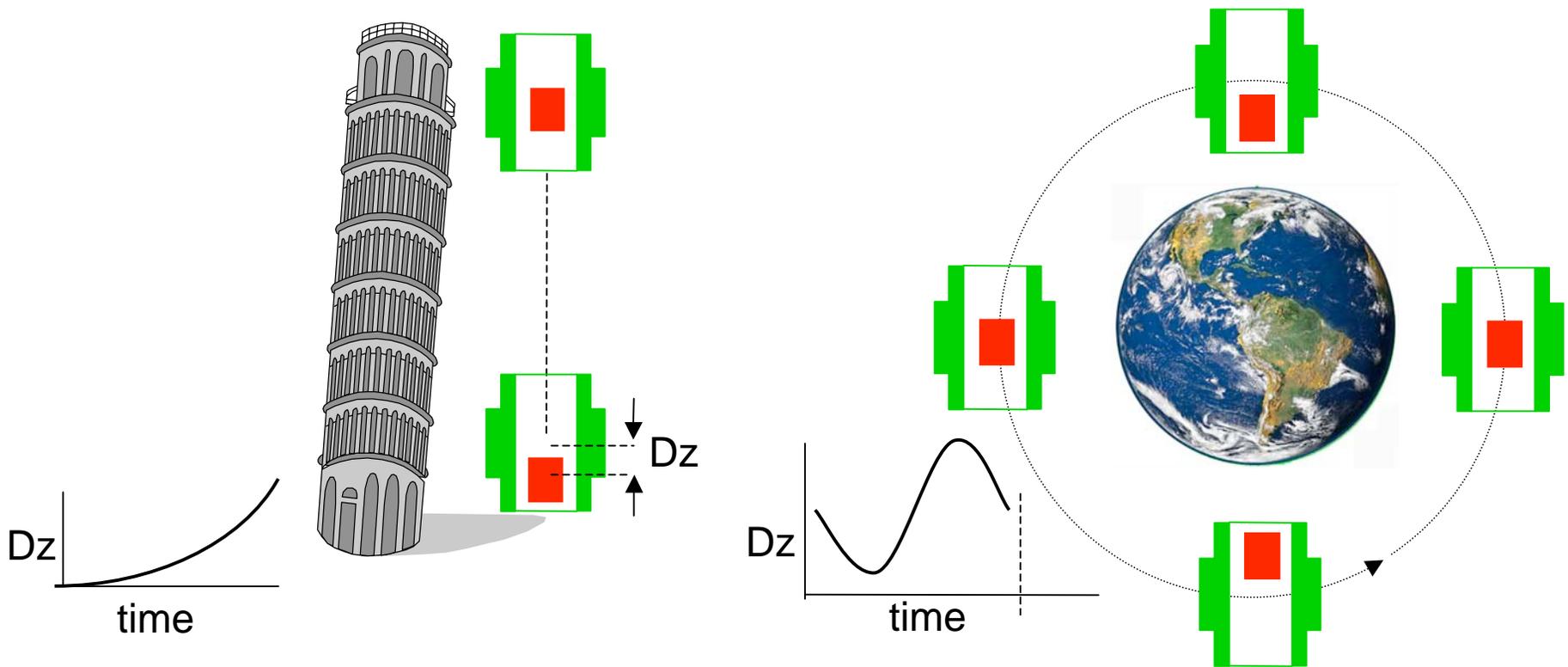
• **STEP Awarded NASA OSS SMEX Phase A Study, w/Euro team, 2002**

- Industrial Spacecraft Study Completed by ASTRIUM UK
- Not selected for flight

• **Current Status: 2nd year of 3 year Technology Development under MSFC**

Advantage of Space

Drag Free Control => Seismically Quiet Environment
Earth as Gravity Source, x1000 over ground based torsion pendula



Orbiting drop tower experiment { * More time for separation to build
* Periodic signal

How to achieve a seismically Quiet Environment

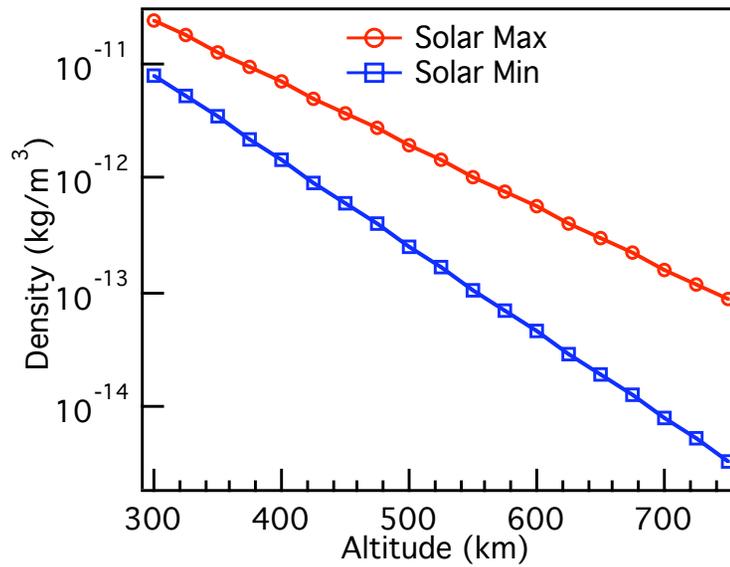
STEP/MiroSCOPE Requirement: Provide a quiet platform for experiment
 $2 \times 10^{-14} \text{ m/s}^2$ at signal frequency averaged over 20 orbits

Free-flyer satellites above 500 km typically experience 10^{-7} to 10^{-8} g
acceleration environments

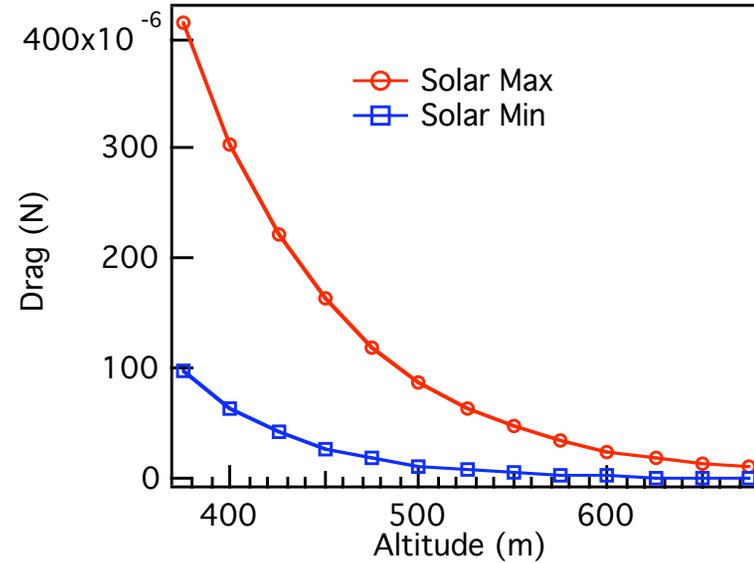
this does not include internally induce vibrations from moving parts
gyros, momentum wheels,

Aboard the International Space Station acceleration noise has been
measured at 10^{-4} g

Atmospheric Environment



Atmospheric density



Deterministic drag from a standard model

$$F_D = 1/2 \rho C_D A v^2$$

STEP Drag Environment

- Disturbance forces and torques exerted on a ~1000 kg, 1m³ satellite at ~600 km orbit

Spacecraft Disturbances		
Source	Translation (N)	Torque (N·m)
Aerodynamic Drag	$4.5 \cdot 10^{-5}$	$9 \cdot 10^{-6}$
Magnetic	Negligible	$3.2 \cdot 10^{-4}$
Gravity Gradient	$3 \cdot 10^{-4}$	$1.8 \cdot 10^{-4}$
Radiation Pressure	$3.3 \cdot 10^{-5}$	$9.3 \cdot 10^{-6}$

- For a 1000kg spacecraft acceleration $a \sim 4 \times 10^{-4} \text{N} / 1000 \text{kg} = 4 \times 10^{-8} \text{ g}$
- So some form of disturbance reduction is needed.

Drag Free Technology

Control Spacecraft to follow an inertial sensor

Reduce disturbances in measurement band

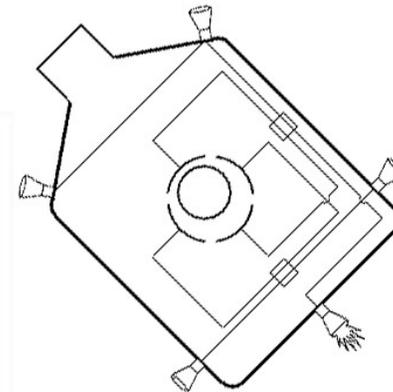
- Aerodynamic drag

- Magnetic torques

- Gravity Gradient torques

- Radiation Pressure

Spacecraft Follows a purely Gravitational Orbit



Drag Free History

Drag-Free Satellites have flown successfully

TRIAD I : Johns Hopkins Applied Physics Laboratory Navy Transit Navigation System
Launched September 2, 1972
Polar Orbit at 750 km
Mission Lifetime over one year
DISCOS - Disturbance Compensation System - built by Stanford University
3 axis translation control

And Now Also GP-B

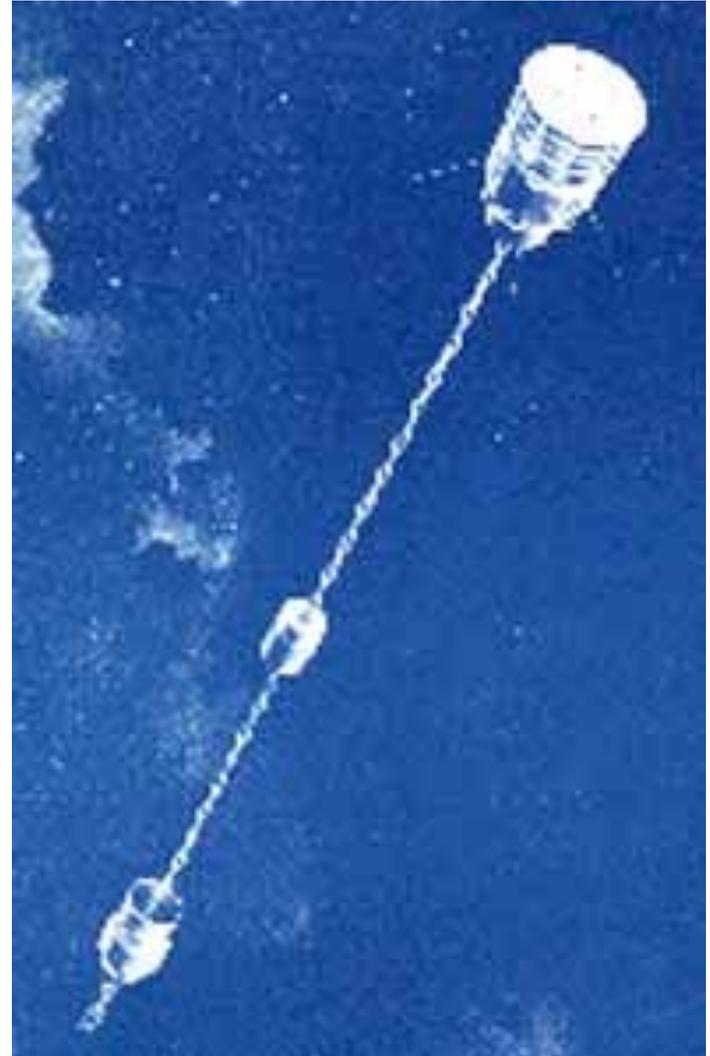
3 axis translation control
3 axis attitude control

DISCOS Performance

- Electrostatic Sensing of Proof Mass
- Pressurized gas “On-Off” Thrusters
- 3 Axis Translation Control
- Acceleration levels were below 5×10^{-12} g

averaged over 3 days

- limited by tracking data and earth gravity model

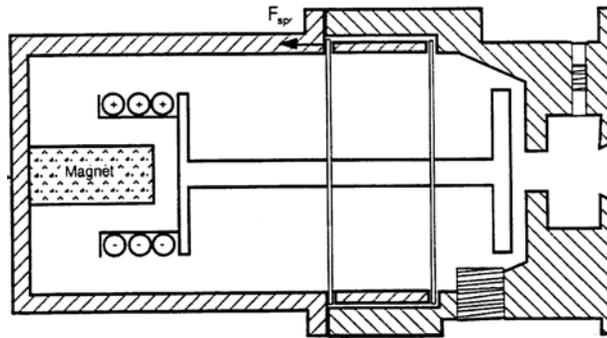


Drag Free Control

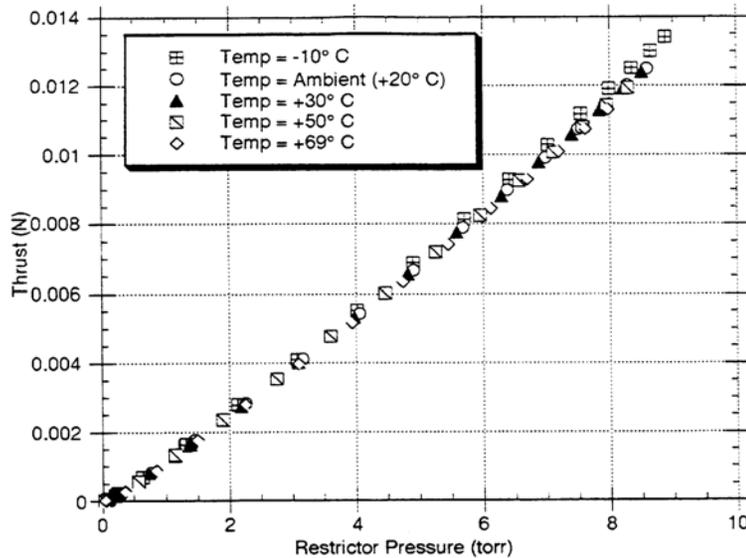
- 7 variables are controlled using the thruster actuators
 - 3 degrees of freedom translation
 - 3 degrees of freedom attitude
 - dewar bath temperature via helium exhaust pressure
- STEPs 16 thrusters will be actuated independently allowing control of all 7 variables
 - helium mass flow in excess of thrust needed for ATC is “null dumped” by sending ~ equal amounts to all thrusters
- Thruster nozzle throat diameter is sized conservatively to allow excess flow

Ref: *The design of a propulsion system using vent gas from a liquid helium cryogenic system*,
P.J.Wiktor, Stanford University PhD thesis, 1992

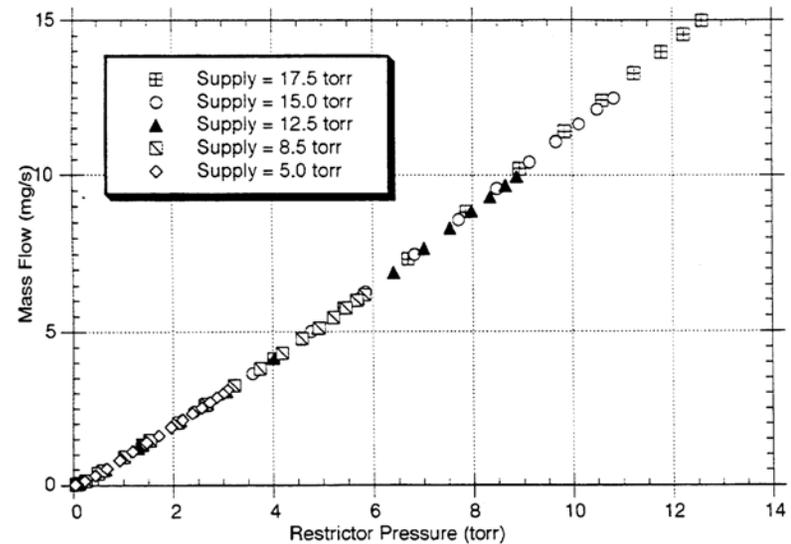
Thruster Pressure Feedback



- Thruster cross-sectional diagram
- Feedback control of restrictor pressure



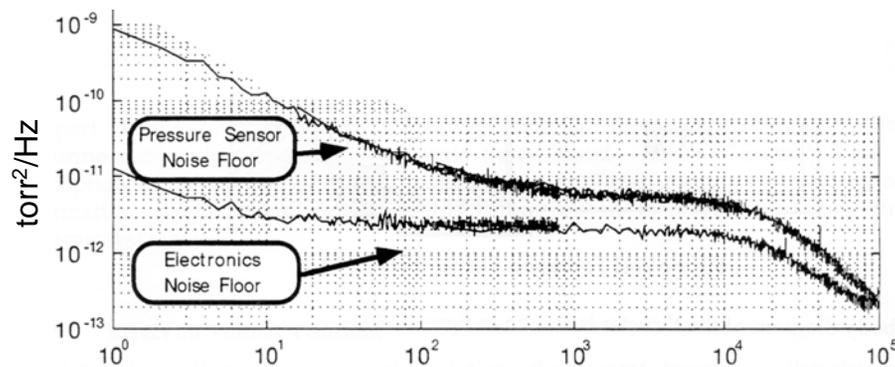
Thrust vs. Restrictor-Pressure at various supply pressures for GPB



Mass flow vs. restrictor pressure at various temperatures for GPB

Thruster Noise

Pressure Sensor Noise Spectrum¹



- Thruster noise dominated by pressure sensor noise
- Thruster Noise:

$$5 \times 10^{-7} \frac{N}{\sqrt{Hz}} \quad \text{at 1 Hz}$$

- Lower frequency thruster noise rejected by DFC

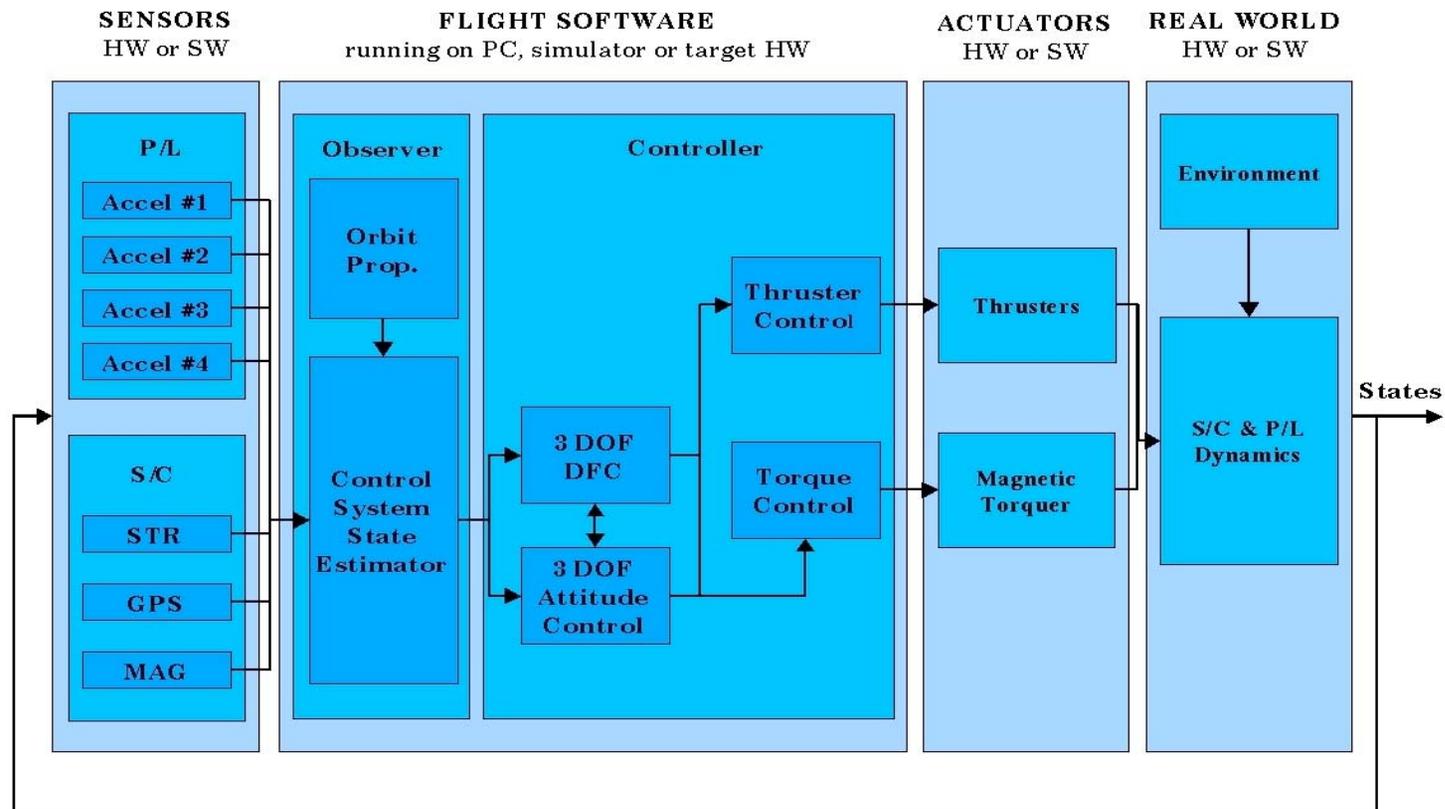
Plunger-motion

- Disturbance attenuated by large spacecraft / plunger mass ratio
- Addressed in Drag-free Control analysis and STEP Error analysis

¹ pg 67, GPB Helium Thruster System Design and Documentation. SCSE-04, Part 11, Rev.B.
IHP 2006 Experimental Tests of General Relativity Mester

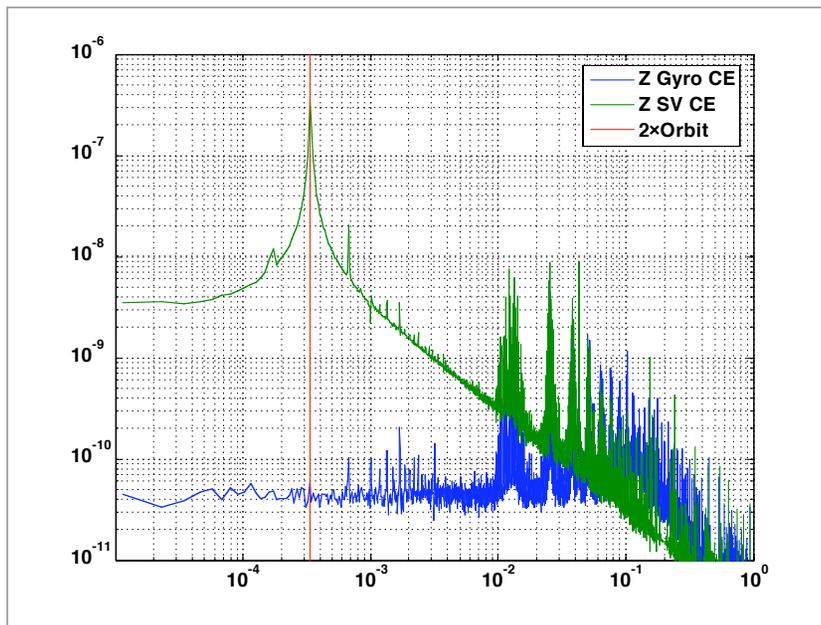
Drag Free Controller

- Algorithm development using engineering simulator based on test-mass and satellite dynamics simulator.
- Algorithm test and flight software design and coding using engineering simulator.
- Flight software verification using end-to-end software simulator.
- Hardware-in-the-loop-tests for flight software running on the target hardware.



GPB technology Transfer: Advanced Simulator

- **Simulator effectiveness for on-orbit operation:**
 - ◆ Pre-launch V&V of drag-free and GSS (EPS) software, hardware.
 - ◆ Debug of GSS suspension issues (gyro charge).
 - ◆ Rectification of ATC/GSS/Dewar coupling (slosh).
 - ◆ Verification of post-launch ATC software changes.
 - ◆ On-orbit tuning of drag-free controller for optimum performance.

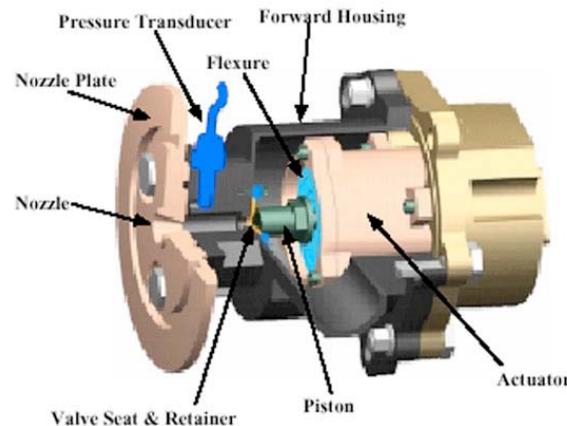


On-orbit Performance - met requirements

- Performance at 4×10^{-12} g level between 0.01 mHz and 10 mHz in inertial space.
- Suppression of gravity gradient acceleration by a factor of $\sim 10,000$.

Drag-Free Implementation for STEP

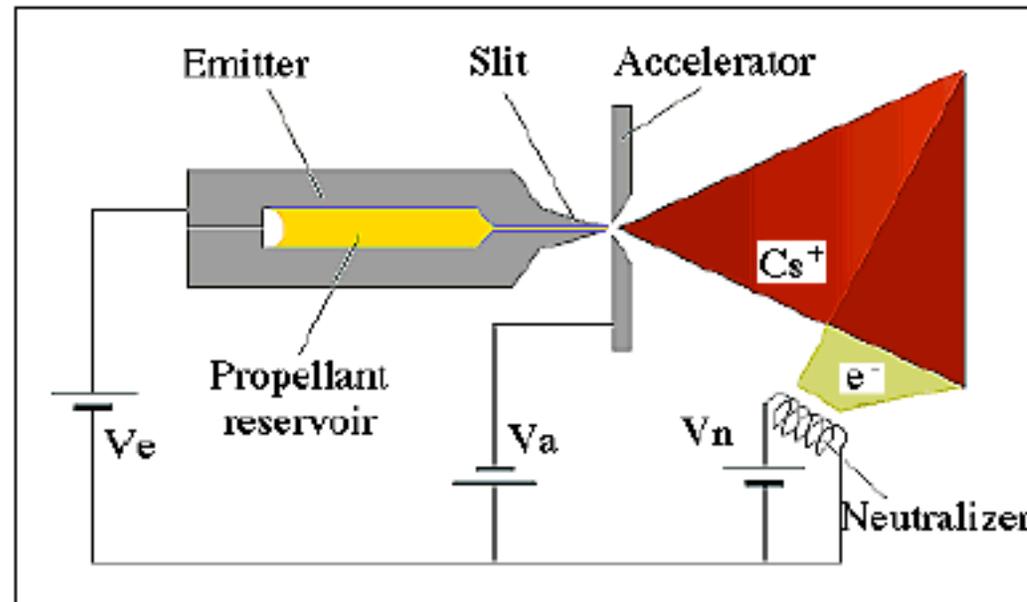
- Electrostatic and SQUID Sensing of Test Mass Common Modes
- Control Algorithm development at ZARM and Stanford
- He gas proportional thrusters and drive electronics - GP-B Program,
- Specific impulse is constant over a range of nozzle diameters
- 10 μN - 10mN thrust range (Less than a breath)
- Gas supply already exists - He cryogen boil off



GP-B Proportional Thruster Schematic

Drag-Free Implementation for Microscope

- Electrostatic Sensing of Test Mass Common Modes
- Control Algorithm development at ONERA
- FEEP thrusters -Field Emission Electric Propulsion and drive electronics, ESA contribution
- $1\mu\text{N}$ - 1mN thrust range



FEEP Thruster Concept

Liquid Metal propellant - Cesium (m.p.= 28.4 °C),
Rubidium (m.p.= 39 °C)
Indium (m.p.= 156 °C)

Small channel produces 1 μ m radius of curvature in liquid

Electric field generated by voltage difference between the emitter and an accelerator electrode

Atoms at the tip spontaneously ionize - ion jet is extracted by the electric field,

An external source of electrons (neutralizer) maintains electric neutrality

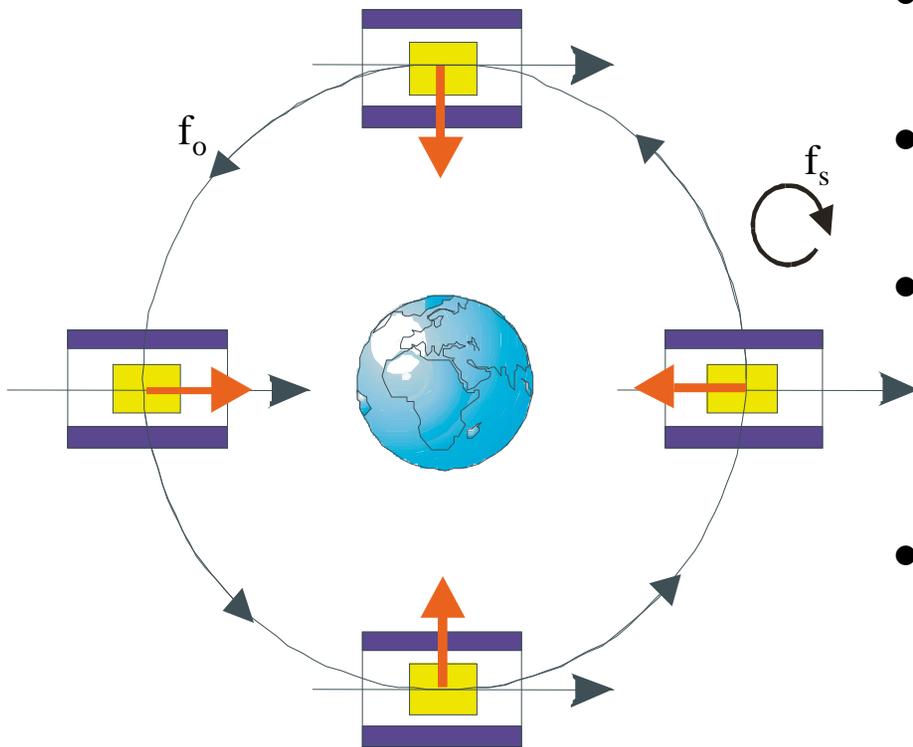
Advantages - High specific impulse ($I_{sp} = 6000 - 10000$ s), no moving parts

Disadvantage - high specific power (about 60 mW/ μ N),

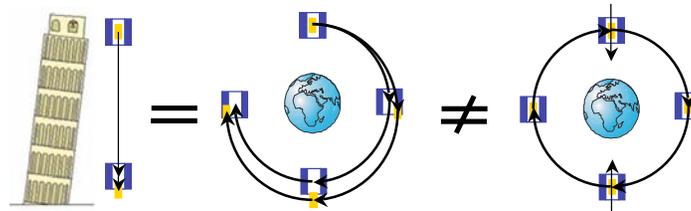
Equivalence Principle in Space

Microscope Concept

slides from Pierre Touboul



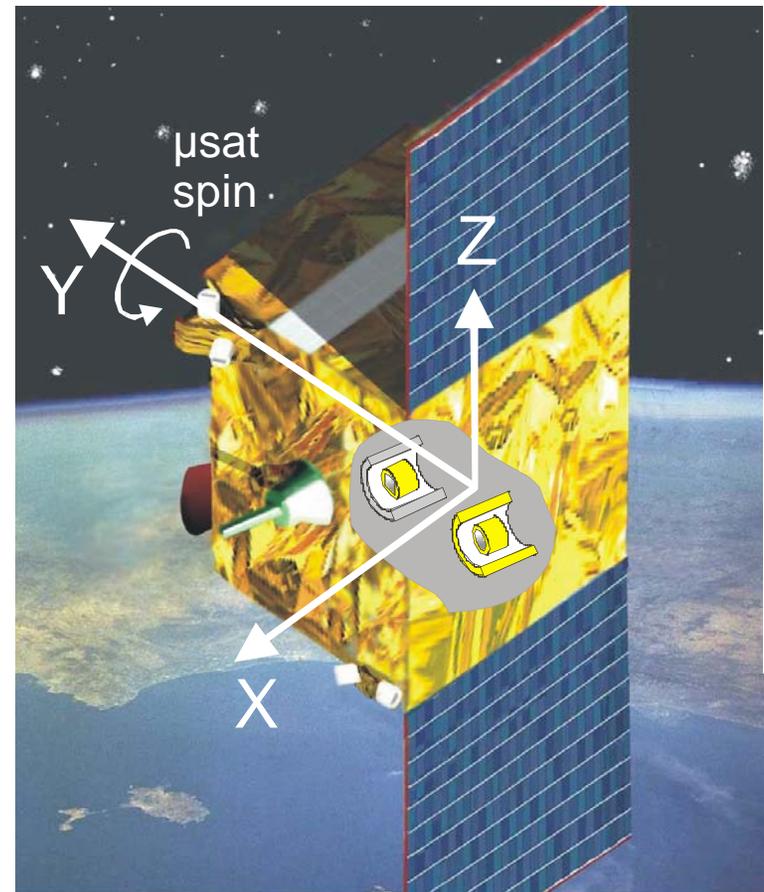
Platinum
 Titanium



- Two masses of different materials maintained on the same orbit ($<10^{-11}\text{m}$) by electrostatic forces
- An EP violation is indicated by a difference between the required forces
- Circular and heliosynchronous orbit ($e < 5 \times 10^{-3}$)
 - Thermal stability
 - Earth gravity gradient stability
 - 730 km altitude
- Two test modes:
 - inertial: $f_{\text{ep}} = f_{\text{orb}} = 1.7 \cdot 10^{-4}\text{Hz}$
 - spin: $f_{\text{ep}} = f_{\text{orb}} + f_{\text{spin}} = 7.8 \cdot 10^{-4}\text{Hz}$

Microscope Payload and Satellite Description

- On board a MYRIADE Microsatellite
- Launch in 2009-2010
- Mission duration of 12 months
- Two differential accelerometers
 - ◆ Two masses of identical material (PtRh) for test accuracy verification
 - ◆ Two masses of different material (PtRh/TA6V) for EP test
- Passive thermal control
- Electrical thrusters: FEEP (ESA)
 - ◆ Or Cold Gas, Trade Study underway
- Drag-Free and Attitude Control System (DFACS)

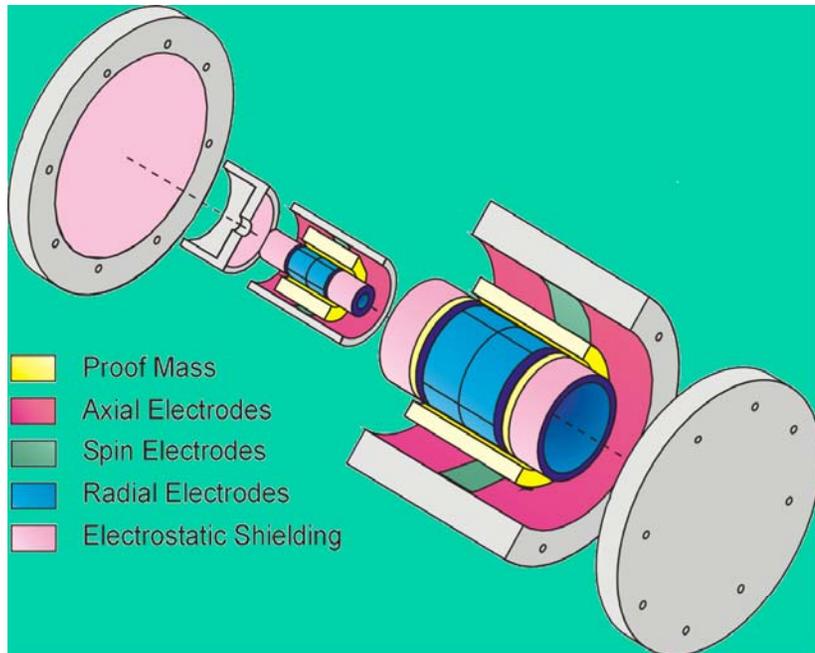


courtesy CNES

To obtain a test resolution better than 10^{-15}

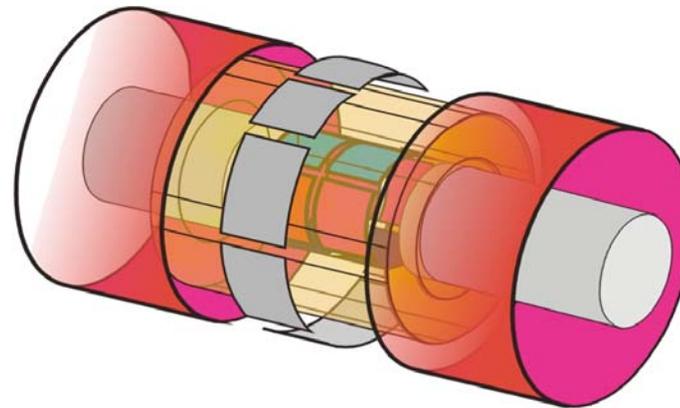
Accelerometer resolution $< 10^{-12} \text{m/s}^2/\text{Hz}^{1/2}$

Microscope Inertial Sensor Configuration



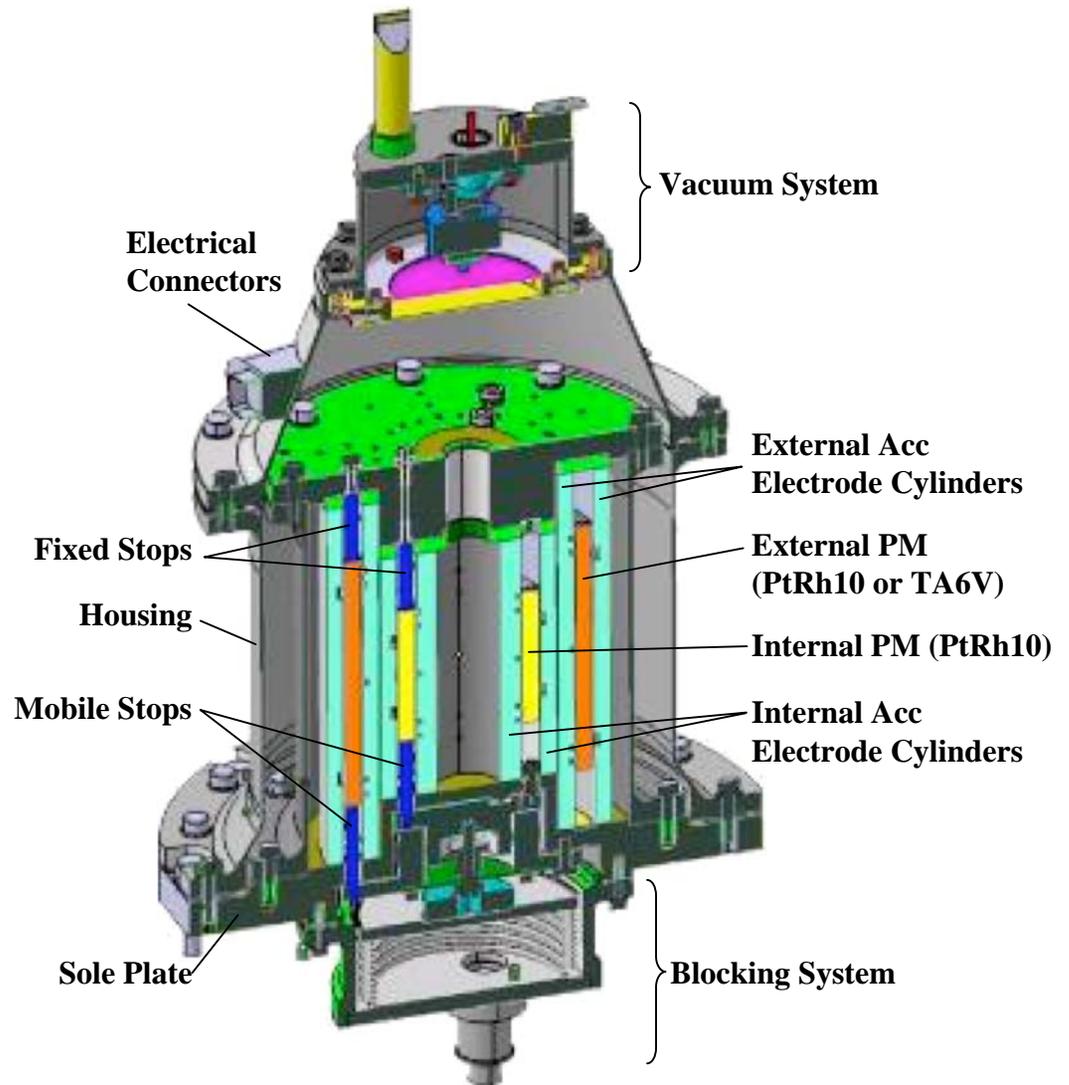
- **Two coaxial, concentric cylindrical inertial sensors**
 - **Common centers of mass ($<20 \mu\text{m}$)**
 - **Masses centered in silica electrode cage**
- **Electrodes work in pairs for:**
 - **Position capacitive sensing**
 - **Gap variation (radial axes)**
 - **surface variation (sensitive axis)**
 - **Electrostatic control of the 6 degrees of freedom of each mass**

- **$\varnothing 5 \mu\text{m}$ gold wire for:**
 - **PM charge control**
 - **Capacitive sensing**
- **Specific blocking mechanism with removable fingers**
- **Getter pumping**

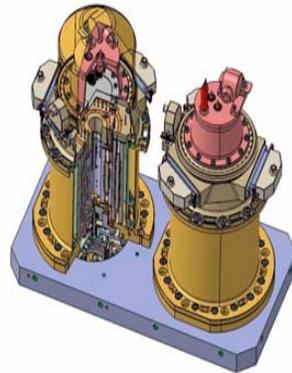
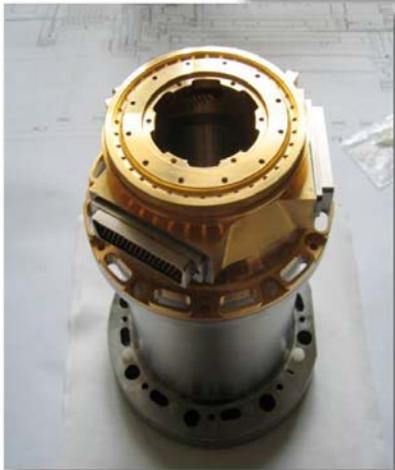
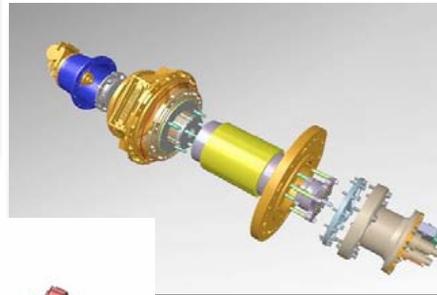
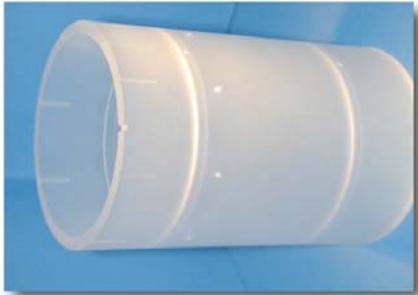


Microscope Sensor Unit

- **Cylindrical PM**
 - ◆ Identical moment of inertia along 3 axes to minimize gravity gradient effect
- **Electrode cylinders in gold-plated silica for thermal stability**
- **Retractable stops to block the masses during launch**
- **Getter material and tight housing to maintain low vacuum**
- **Invar housing for magnetic shielding**



Microscope Sensor technology



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Experimental Tests of General Relativity

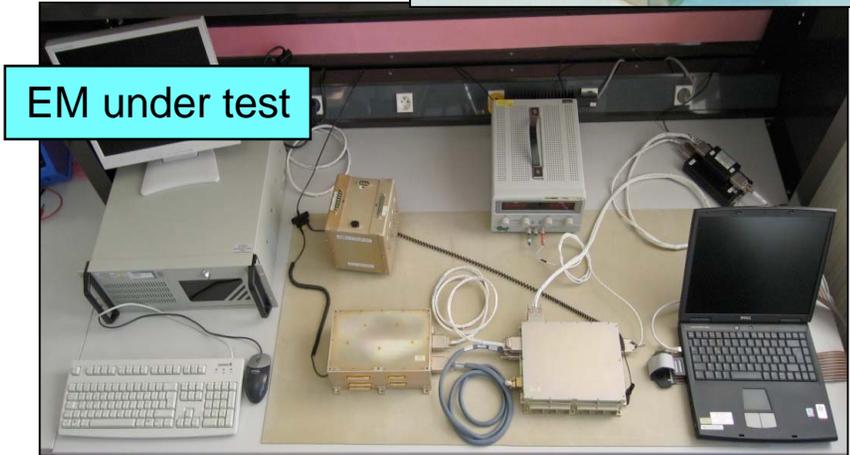
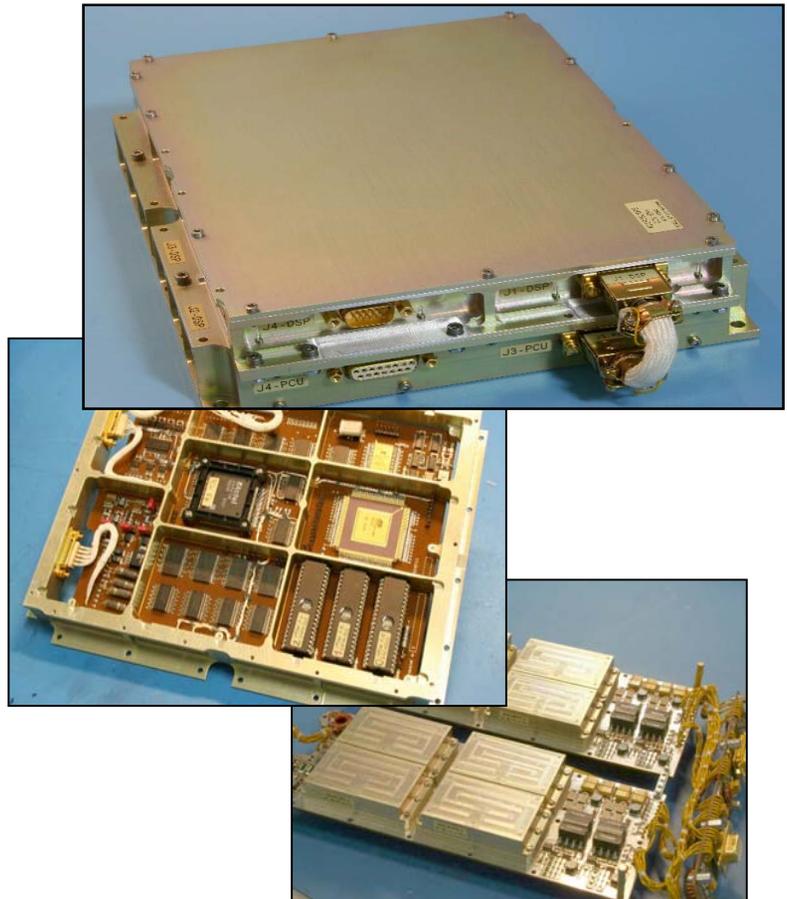
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Microscope Engineering Model Electronics

Front End Electronics Unit
(capacitive sensing & actuation)



Interface & Control Unit
(Control laws, DSP, DC/DC converters)



EM under test

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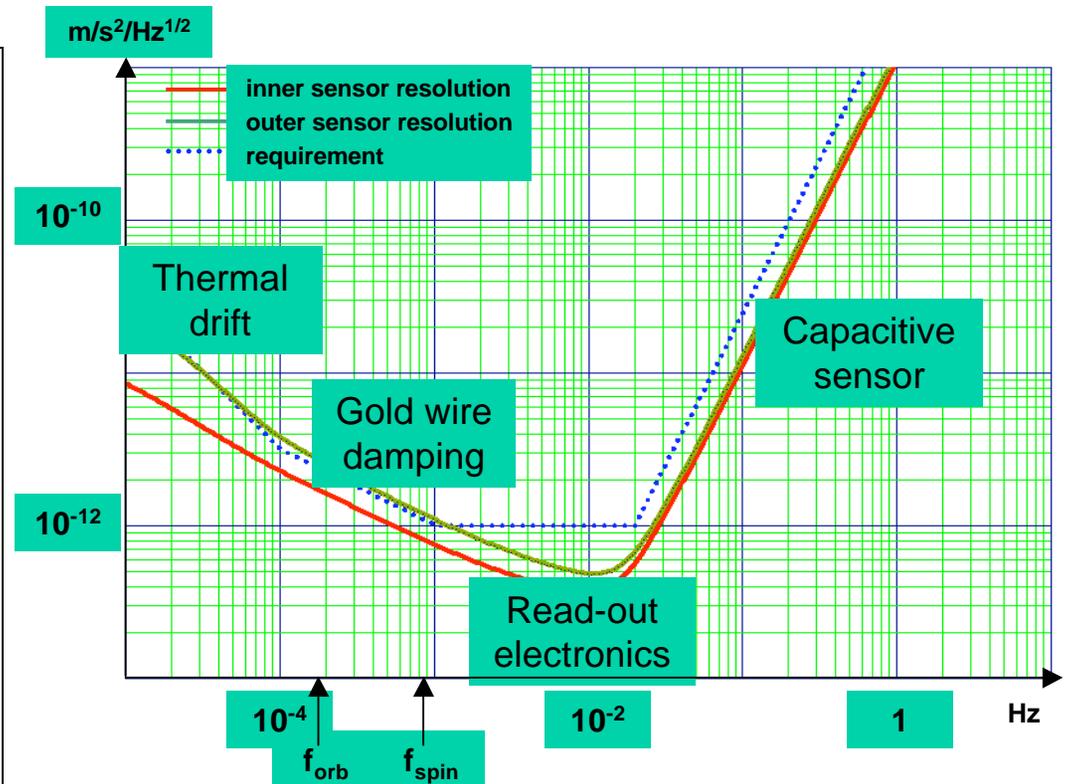
Experimental Tests of General Relativity

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Microscope Expected Accuracy

- Computed on the instrument definition after PDR :
 1. All functions specified and major ones verified on breadboard
 2. Trade-off between instrument performance, in orbit accommodation and operation, in orbit calibration, in order to achieve 10^{-15} test accuracy

- Selected Configuration :
 - Instrument geometry and materials
 - Electronics functions and performance
 - Environment (acceleration, magnetic, thermal, gravitational,...)
- Instrument major parameters :
 - Bias (value and fluctuations)
 - Scale factor (value and fluctuations)
 - Bias thermal sensitivity
 - Scale factor thermal sensitivity
 - Noise
- Instrument in orbit accommodation :
 - Attitude and Orbit control, Earth gravity gradients, calibration,...



STEP International Collaboration

Stanford University -- PI Francis Everitt

Marshall Space Flight Center

University of Birmingham, UK

ESTEC

FCS Universität, Jena, Germany

Imperial College, London, UK

Institut des Hautes Études Scientifiques, Paris

ONERA, Paris, France

PTB, Braunschweig, Germany

Rutherford Appleton Laboratory, UK

University of Strathclyde, UK

Università di Trento, Italy

ZARM, Universität Bremen, Germany

STEP Mission

6 Month Lifetime

Sun synchronous orbit, $i=97^\circ$

550 Km altitude

Drag Free control w/ He Thrusters

Cryogenic Experiment

Superfluid Helium Flight Dewar

Aerogel He Confinement

Superconducting Magnetic Shielding

4 Differential Accelerometers

Test Mass pairs of different materials

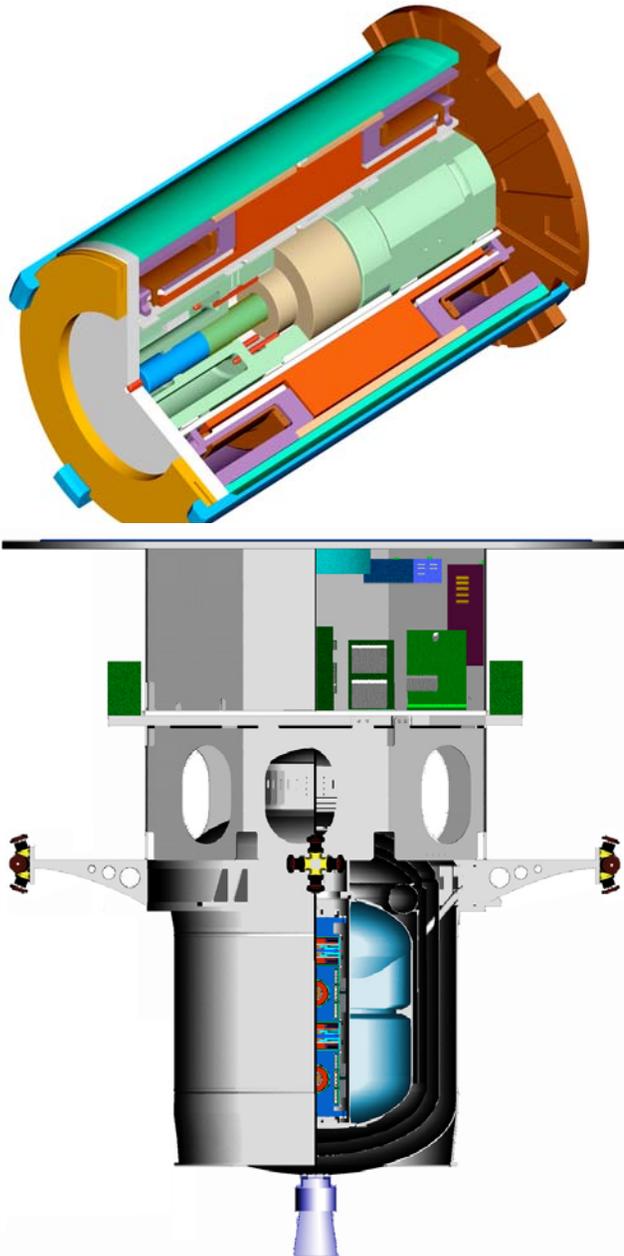
Micron tolerances

Superconducting bearings

DC SQUID acceleration sensors

Electrostatic positioning system

UV fiber-optic Charge Control

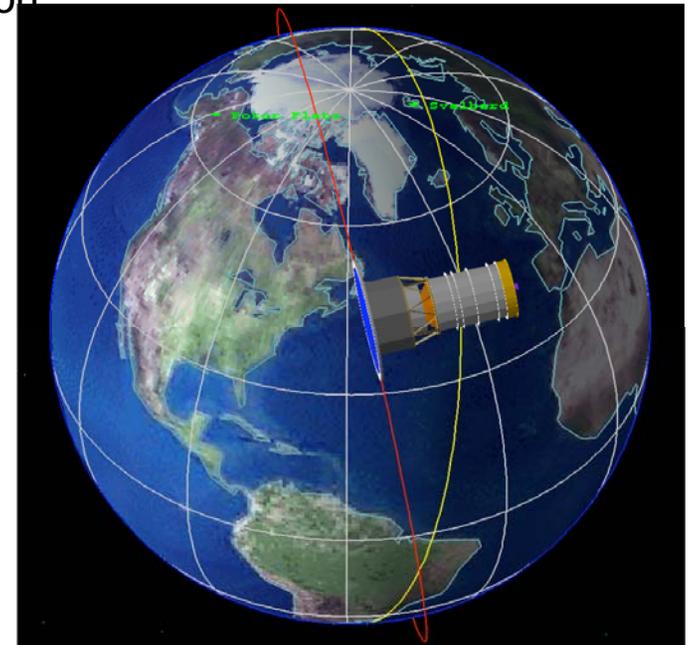


STEP Status

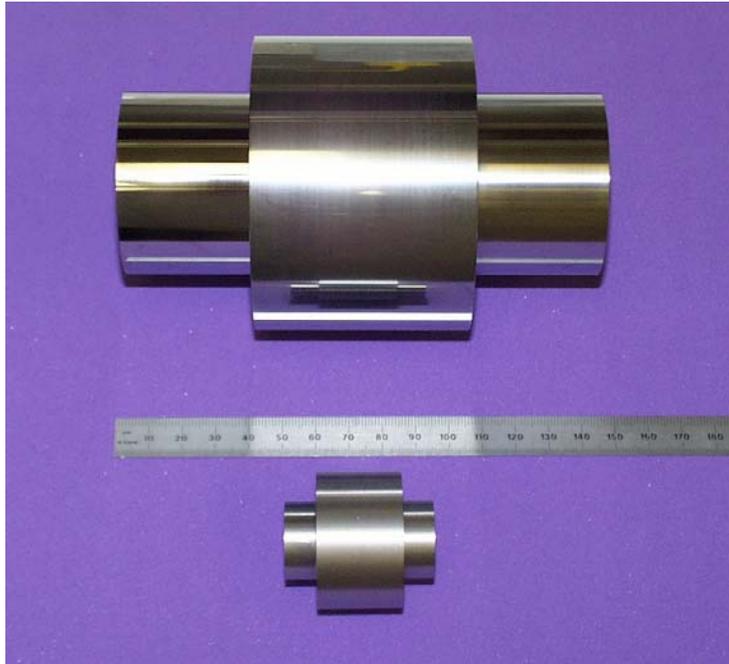
2006: Second year of 3 year Technology Program under NASA MSFC

STEP TP Goals:

- Integrated ground test of prototype flight accelerometer
 - ◆ Fabricate prototype flight instrument
 - ▶▶▶ Differential accelerometer
 - ▶▶▶ Cryogenic electronics
 - ▶▶▶ Quartz block mounting structure
- Dewar /Probe Design
 - ◆ LMMS design study with Dewar/ Probe Interface definition
 - ◆ Probe/Instrument Interface definition
 - ◆ Aerogel Implementation
- Systems Study
 - ◆ Update Error Budget
 - ◆ Requirements flowdown
 - ◆ Electronics requirements review/ GP-B heritage study
- Space Vehicle Dynamics
 - ◆ Drag Free and Attitude Control design
 - ◆ Accelerometer Dynamics simulator
 - ◆ On-Orbit Setup algorithm design with ops interface



Test Masses



Dimensions selected to give 6th order insensitivity to gravity gradient disturbances from the spacecraft

Micron tolerances

Test Mass should be as ‘different’ as possible

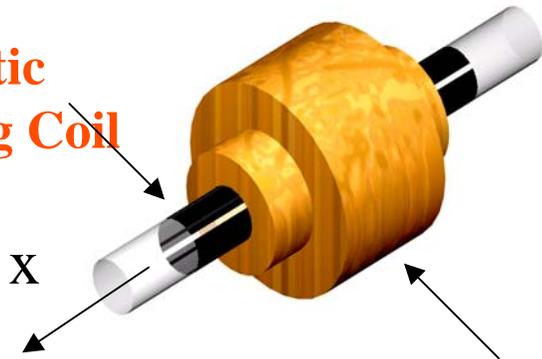
Material	Z	N	$\left(\frac{N+Z}{\mu} - 1\right)10^3$ Baryon Number	$\frac{N-Z}{\mu}$ Lepton Number	$\frac{Z(Z-1)}{\mu(N+Z)^3}$ Coulomb Parameter
Be	4	5	-1.3518	0.11096	0.64013
Si	14	14.1	0.8257	0.00387	2.1313
Nb	41	52	1.0075	0.11840	3.8462
Pt	78	117.116	0.18295	0.20051	5.3081

Damour C&QG 13 A33 (1996)

Magnetic Bearing

SUPERCONDUCTING CIRCUITS ON CYLINDERS

Magnetic Bearing Coil



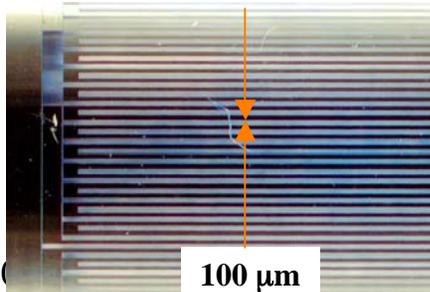
- **UV Laser Patterning System**

- Sub-micron Resolution on Outside Surface
- Micron Resolution on Inside Surface

Superconducting Magnetic Bearing



160 mm

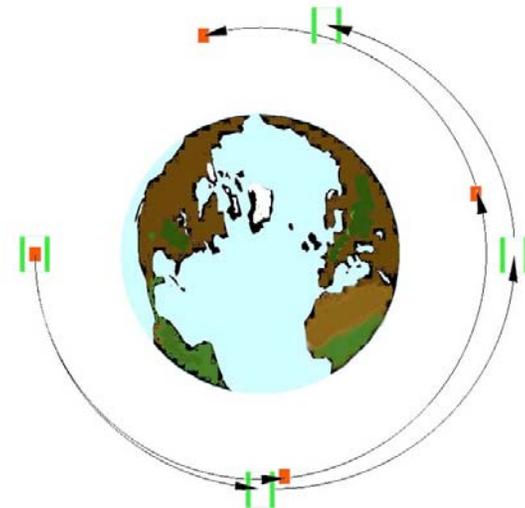


IHP 20

100 μm

ental Tests of General Relativity

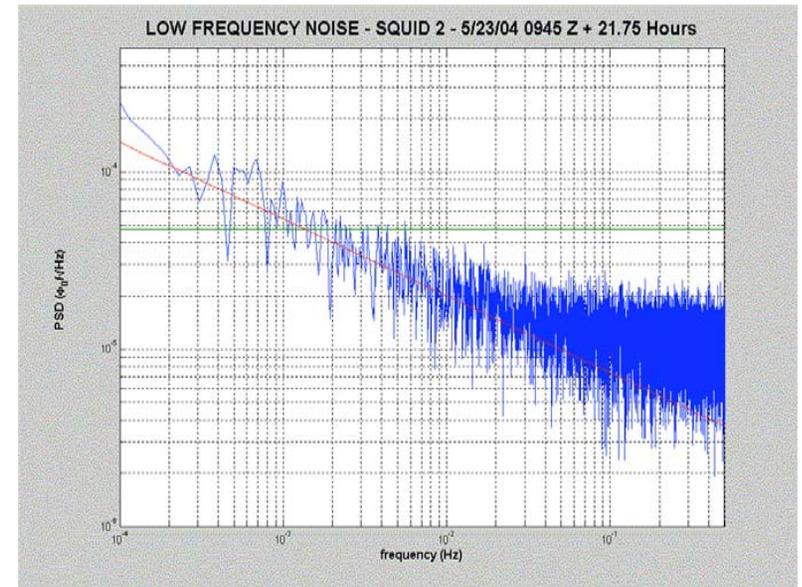
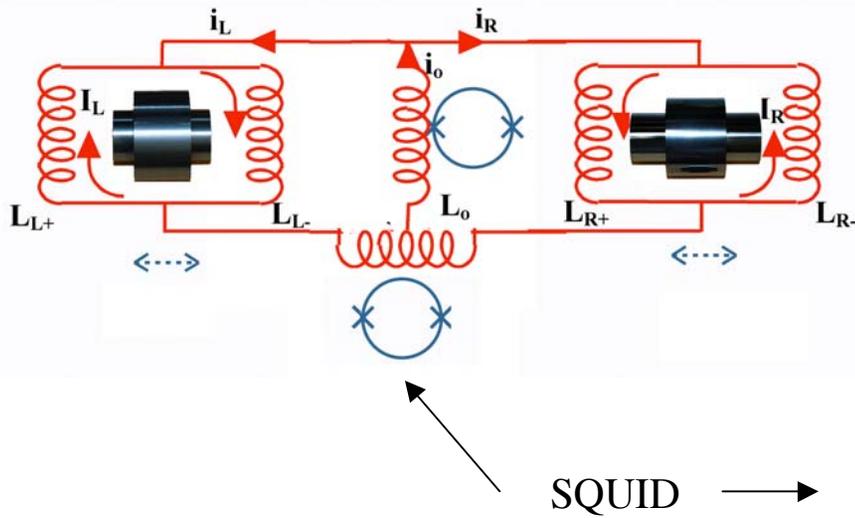
Mester



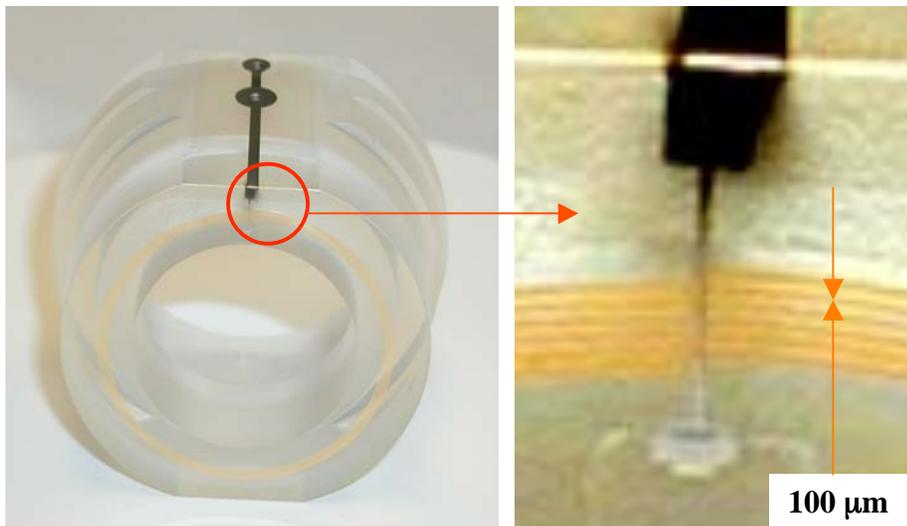
1 d constraint yields periodic signal

SQUID DISPLACEMENT SENSOR

Differential Mode Sensor Yields a Direct Measure of Differential Displacement



GP-B On-Orbit SQUID Noise

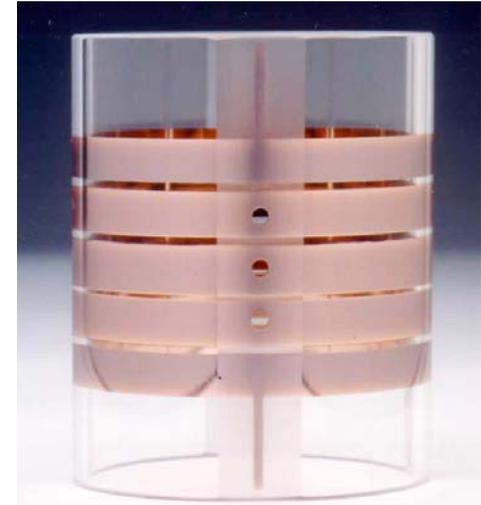
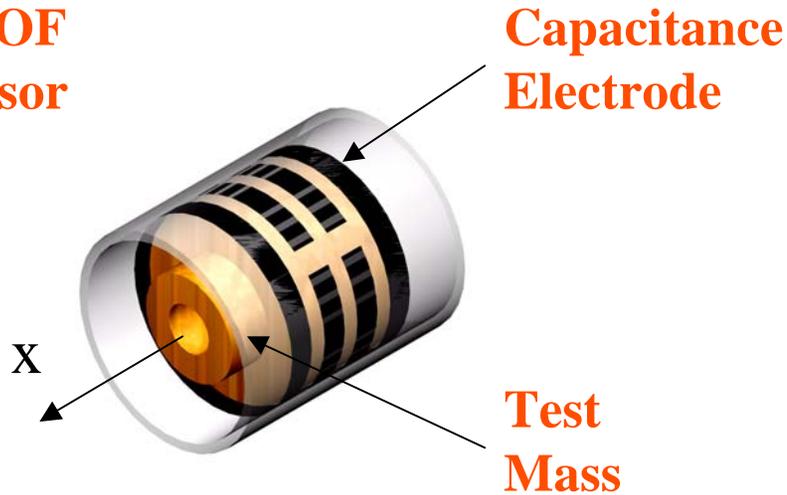


Differential Acceleration Sensitivity $4 \times 10^{-19} g_0$
 Natural Frequency 10^{-3} Hz
 Displacement Sensitivity 10^{-13} m

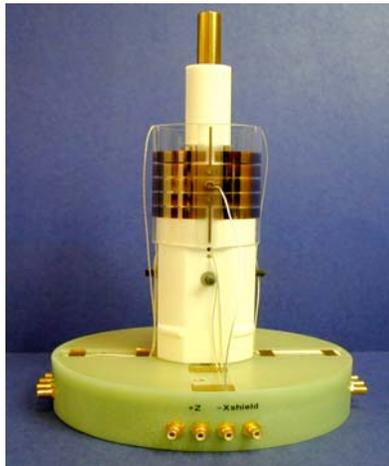
On Orbit performance meets STEP requirements

Electrostatic Positioning System

6 DOF
Sensor



Capacitance Displacement Electrodes



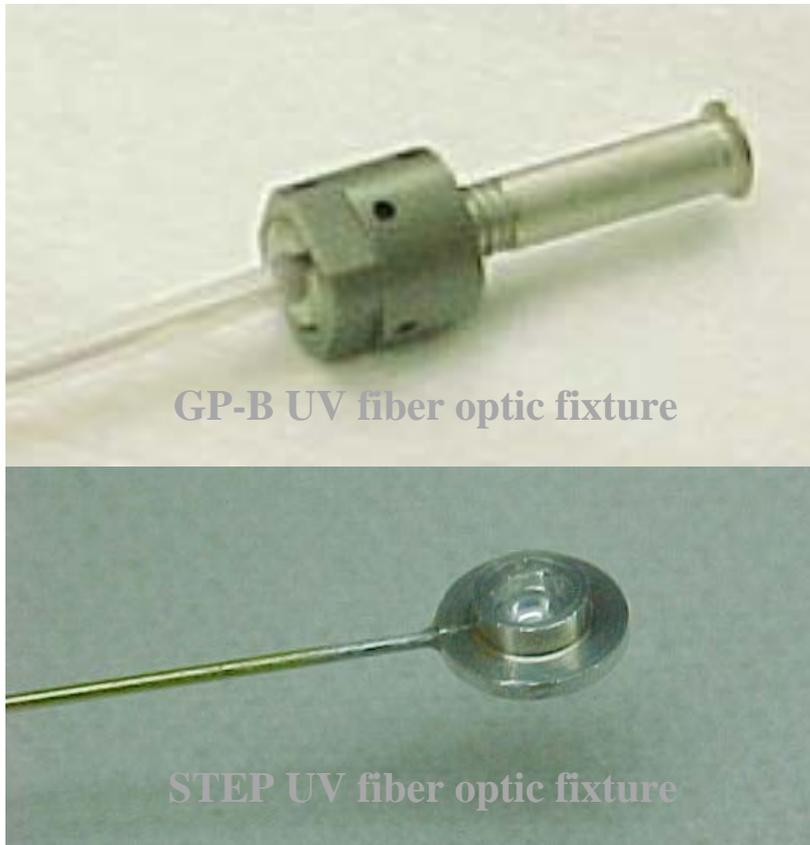
Inner electrode structure
surrounding test mass.
Electronic hardware
interface measurements
underway since April 2001



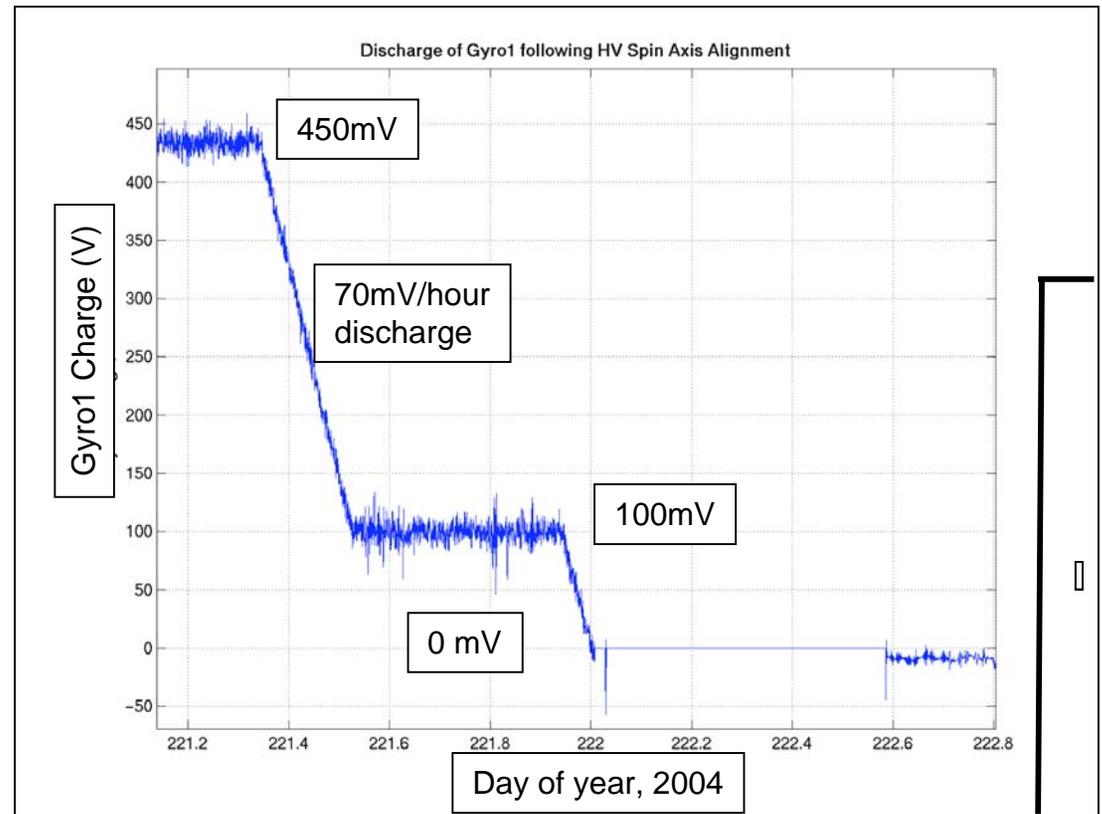
ONERA EPS Electronics

UV Charge Control

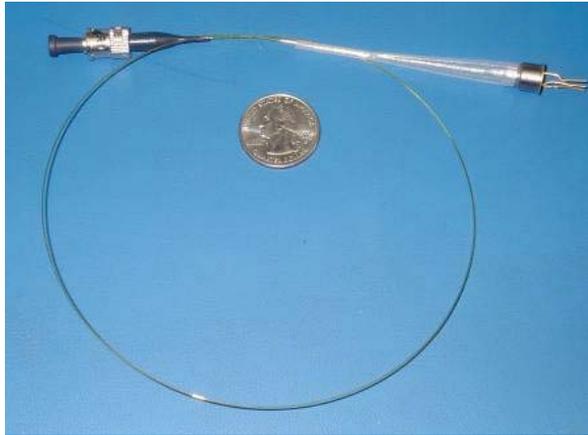
System Components: UV Light source, fiber optic, and bias electrode



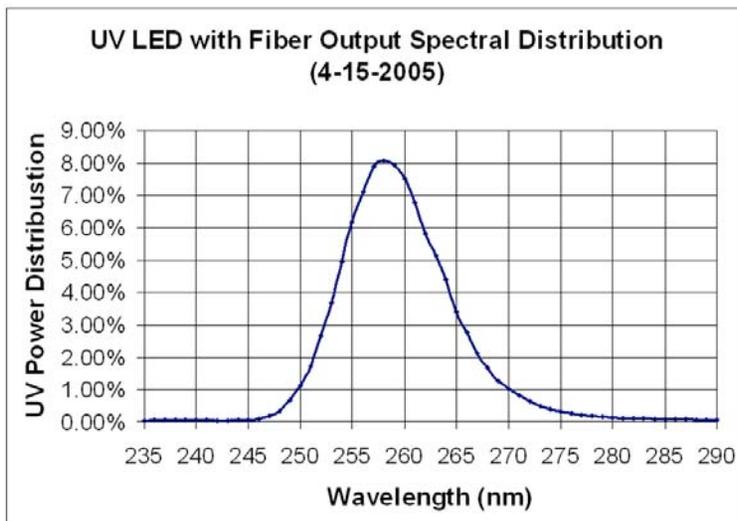
Discharge of GP-B Gyro1



LED Deep UV Source for Charge Management



- **UV LED System Dev By SU LISA Team**
 - **Light weight**
 - **Low electrical power**
 - **Compact, robust**
 - **Fast modulation**



Peak wavelength:

257.2 nm, comparable to Hg line 254 nm

FWHM:

12.5 nm, good photoemission for Au coatings

Total UV power:

0.144 mW, sufficient for charge management

K. Sun, B. Allard, S. Williams, S. Buchman, and R. L. Byer, "LED Deep UV Source for Charge Management for Gravitational Reference Sensors," *Class. Quantum Grav.* 23 (2006) S141-S150

Space Flight Dewar and Cryogenic Probe

STEP Dewar

Lockheed Martin Design
ID dewar Internal Development
230 liters
> 6 month on-orbit life
1.8 K ambient temperature

Cryogenic Probe

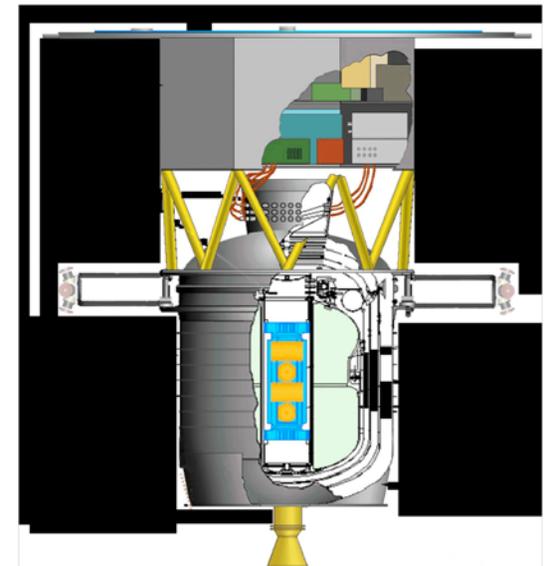
RAL design
He Boil-off Drives Proportional Thrusters
Porous Plug device
Aerogel Tide Control



GP-B Dewar
IHP 2006



GP-B Probe
Experimental Tests of General Relativity

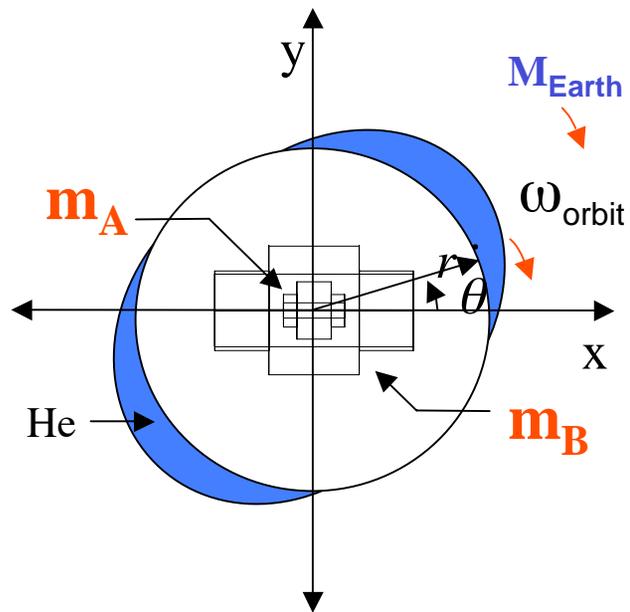
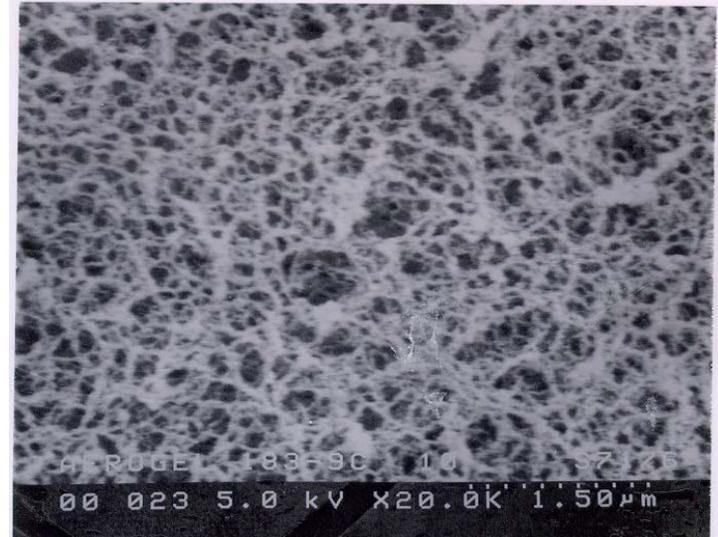


STEP Spacecraft w/ Dewar & Thrusters
Mester

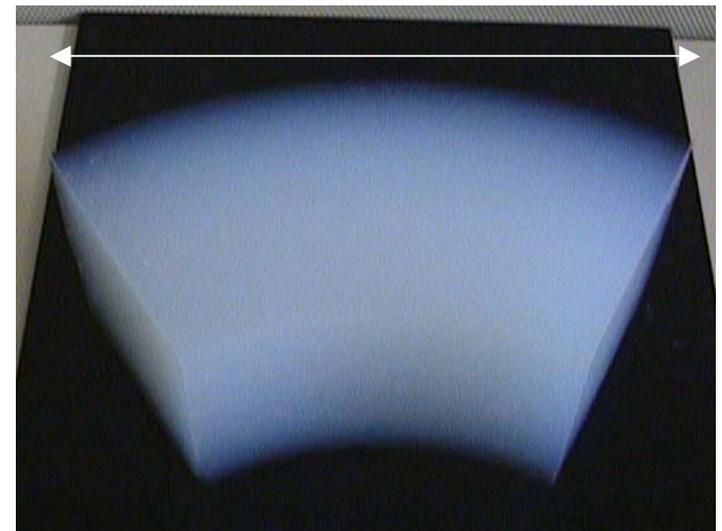
Helium Tide Control

Silica Aerogel Constraint

- large range of void sizes 100 to 1000 nm
- Confines He Even in 1g
- Passed Cryogenic Shake Test at expected launch loads



250 mm



STEP Error Model

Comprehensive error model developed to give self consistent model of whole system

Advances in Space Research, COSPAR Warsaw 2000

Class. Quantum Grav. 18 (2001)

Input: Analytic models of specific disturbances

Environment parameters: earth g field, B field, drag, radiation flux etc.

Instrument parameters: Temp, gradients, pressure, SV rotation rate and stability

Systems parameters: SQUID noise, EPS noise, DFC control laws, Thruster noise, etc.

Outputs: Performance expectation, include sensor noise and disturbances

Set system requirements

Evaluate design tradeoffs

Top 5 Error Sources (Diff. Acceleration Equivalent m/s^2)

SQUID sensor Noise	2.2×10^{-18}	at signal freq, avg over 20 orbits
Nyquist Noise	8.5×10^{-19}	
Radiometer Effect	7.9×10^{-19}	
TM Charge/EPS coupling	6.4×10^{-19}	
Dynamic CM offset	5.4×10^{-19}	

+ > 20 others evaluated ==> STEP will test EP to better than 1 Part in 10^{18}

Conclusion

- Space will enable the advance Equivalence Principle measurements
 - > 5 orders of magnitude
 - 4 accelerometers, each measuring η to 10^{-18} in 20 orbits
- Positive result (violation of EP)
 - Constitutes discovery of new interaction in Nature
 - Strong marker for Grand Unification theories
- Negative result (no violation)
 - Overturns two most credible approaches to Grand Unification
 - Places severe constraints *on new theories*

“Improvement by a factor of around 10^5 could come from an equivalence principle test in space. ... at these levels, null experimental results provide important constraints on existing theories, and a positive signal would make for a scientific revolution.”

Connecting Quarks with the Cosmos: Eleven Science Questions for the New Century (2003) p.162
National Academies Press, the National Academy of Sciences

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- [3] Murphy, T. W. Jr., E. G. Adelberger, J. D. Strasburg, C. W. Stubbs, K. Nordtvedt Testing Gravity via Next-Generation Lunar Laser-Ranging, *Nuclear Physics B (Proc)* 134 (2004) 155–62
- [4] Damour, T.; Polyakov, A.M. The string dilaton and a least coupling principle. *Nuclear Physics B*; 25 July 1994; vol.B423, no.2-3, p.532-58
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