

# Figures of lecture 6

## *Black hole thermodynamics*

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<https://relativite.obspm.fr/blackholes/paris23/>

**PSL graduate programs in Physics and in Astrophysics**  
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# Home page for the lectures

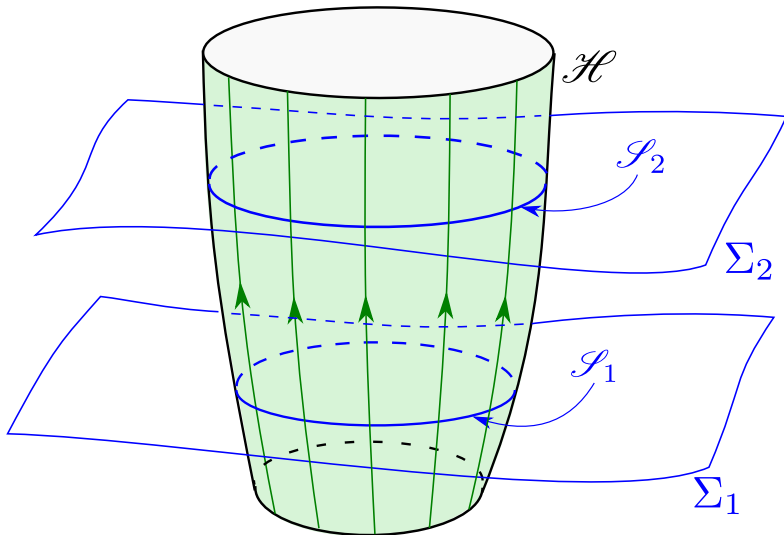
<https://relativite.obspm.fr/blackholes/paris23>

includes

- the lecture notes (draft)
- some SageMath notebooks
- these slides

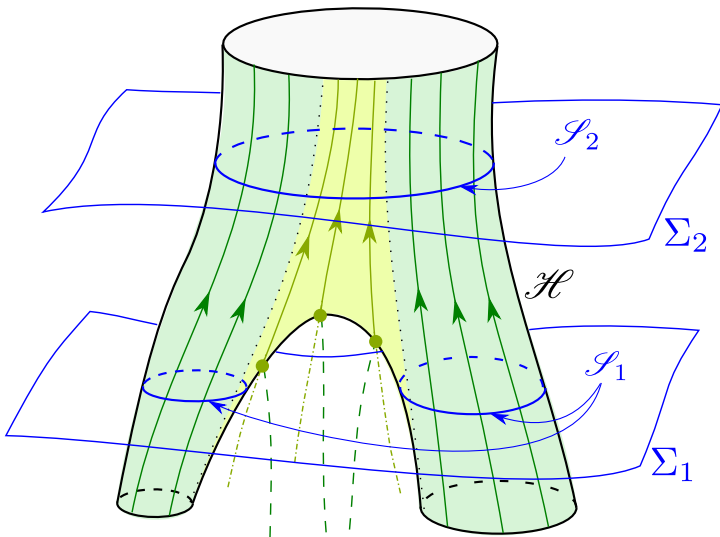
# Area theorem

Smooth part of the event horizon

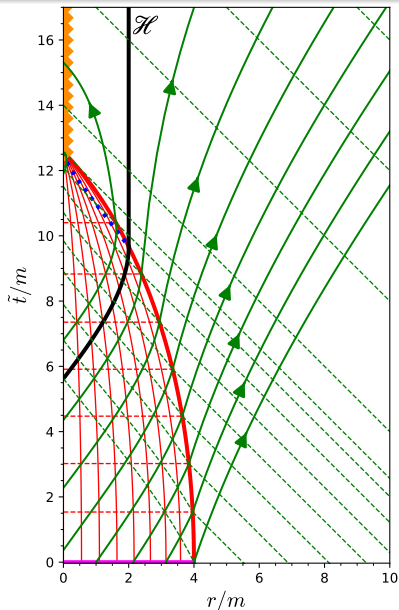


# Area theorem

Generic case



# Horizon growth in the Oppenheimer-Snyder collapse



Collapse of a ball of pressureless matter (dust) initially at rest

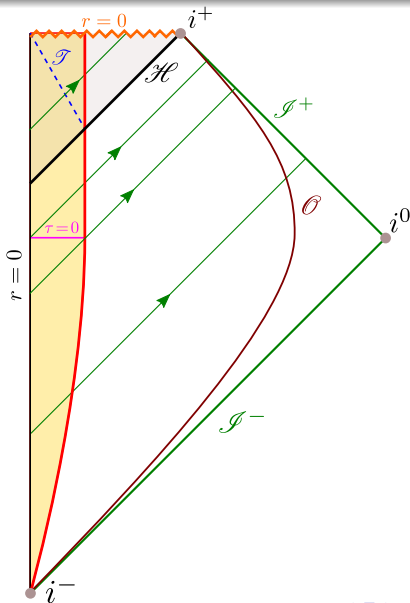
$r$  = areal radius

$\implies$  area of a  $\tilde{t} = \text{const}$  section of  $\mathcal{H}$ :

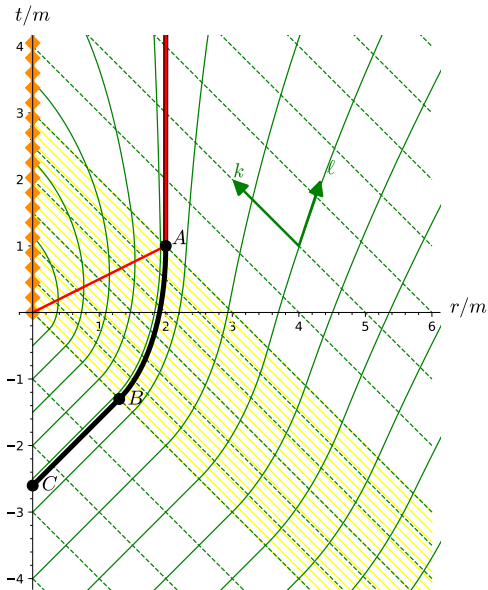
$$A = 4\pi r^2$$

SageMath notebook: [https://nbviewer.org/github/egourgoulhon/BHlectures/blob/master/sage/Oppenheimer\\_Snyder.ipynb](https://nbviewer.org/github/egourgoulhon/BHlectures/blob/master/sage/Oppenheimer_Snyder.ipynb)

# Carter-Penrose diagram of the Oppenheimer-Snyder collapse



# Horizon growth in the Vaidya collapse



Collapse of shell of  
electromagnetic radiation

$r$  = areal radius

$\implies$  area of a  $t = \text{const}$  section  
of  $\mathcal{H}$ :  $A = 4\pi r^2$

SageMath notebook: <https://nbviewer.org/github/egourgoulhon/BHlectures/blob/master/sage/Vaidya.ipynb>

# Carter-Penrose diagram of the Vaidya collapse

