

# Compact objects and strange quark stars

Eric Gourgoulhon

Laboratoire Univers et Théories (LUTH)  
CNRS / Observatoire de Paris / Université Paris Diderot  
F-92190 Meudon, France

[eric.gourgoulhon@obspm.fr](mailto:eric.gourgoulhon@obspm.fr)

<http://www.luth.obspm.fr/~luthier/gourgoulhon/>

**Journées de la division Physique Nucléaire, SFP**

*Du plasma de quarks et de gluons aux étoiles à neutrons*

Nantes, 13-14 May 2008

- 1 Compact stars in general relativity
- 2 Confronting theoretical models and observations: astrophysics as a lab
- 3 The search for strange stars
- 4 Gravitational wave observations

# Outline

- 1 Compact stars in general relativity
- 2 Confronting theoretical models and observations: astrophysics as a lab
- 3 The search for strange stars
- 4 Gravitational wave observations

# Density and compactness

Spherical object of mass  $M$  and radius  $R$

- **density** :  $\rho = \frac{M}{\frac{4}{3}\pi R^3}$

- **compactness** :  $\Xi := \frac{GM}{c^2 R} \sim \frac{|E_{\text{grav}}|}{Mc^2} \sim \frac{|\Phi_{\text{surf}}|}{c^2} \sim \frac{V_{\text{esc}}^2}{c^2} \sim \frac{R_S}{R}$

$E_{\text{grav}}$  = gravitational potential energy;  $\Phi_{\text{surf}}$  = gravitational potential at the surface;  $V_{\text{esc}}$  = escape velocity from surf.;  $R_S$  = Schwarzschild radius

# Density and compactness

Spherical object of mass  $M$  and radius  $R$

- **density** :  $\rho = \frac{M}{\frac{4}{3}\pi R^3}$

- **compactness** :  $\Xi := \frac{GM}{c^2 R} \sim \frac{|E_{\text{grav}}|}{Mc^2} \sim \frac{|\Phi_{\text{surf}}|}{c^2} \sim \frac{V_{\text{esc}}^2}{c^2} \sim \frac{R_S}{R}$

$E_{\text{grav}}$  = gravitational potential energy;  $\Phi_{\text{surf}}$  = gravitational potential at the surface;  $V_{\text{esc}}$  = escape velocity from surf.;  $R_S$  = Schwarzschild radius

$$\Xi = \frac{4\pi G}{3c^2} \rho R^2 \implies \Xi = 6 \times 10^{-10} \left(\frac{R}{\text{m}}\right)^2 \text{ for } \rho = \rho_{\text{nuc}} = 2 \cdot 10^{17} \text{ kg m}^{-3}$$

# Density and compactness

Spherical object of mass  $M$  and radius  $R$

- **density** :  $\rho = \frac{M}{\frac{4}{3}\pi R^3}$

- **compactness** :  $\Xi := \frac{GM}{c^2 R} \sim \frac{|E_{\text{grav}}|}{Mc^2} \sim \frac{|\Phi_{\text{surf}}|}{c^2} \sim \frac{V_{\text{esc}}^2}{c^2} \sim \frac{R_S}{R}$

$E_{\text{grav}}$  = gravitational potential energy;  $\Phi_{\text{surf}}$  = gravitational potential at the surface;  $V_{\text{esc}}$  = escape velocity from surf.;  $R_S$  = Schwarzschild radius

$$\Xi = \frac{4\pi G}{3c^2} \rho R^2 \implies \Xi = 6 \times 10^{-10} \left(\frac{R}{\text{m}}\right)^2 \text{ for } \rho = \rho_{\text{nuc}} = 2 \cdot 10^{17} \text{ kg m}^{-3}$$

proton

$$R = 10^{-15} \text{ m} \implies \Xi \sim 10^{-39}$$

no need for general relativity

# Density and compactness

Spherical object of mass  $M$  and radius  $R$

- **density** :  $\rho = \frac{M}{\frac{4}{3}\pi R^3}$

- **compactness** :  $\Xi := \frac{GM}{c^2 R} \sim \frac{|E_{\text{grav}}|}{Mc^2} \sim \frac{|\Phi_{\text{surf}}|}{c^2} \sim \frac{V_{\text{esc}}^2}{c^2} \sim \frac{R_S}{R}$

$E_{\text{grav}}$  = gravitational potential energy;  $\Phi_{\text{surf}}$  = gravitational potential at the surface;  $V_{\text{esc}}$  = escape velocity from surf.;  $R_S$  = Schwarzschild radius

$$\Xi = \frac{4\pi G}{3c^2} \rho R^2 \implies \Xi = 6 \times 10^{-10} \left(\frac{R}{\text{m}}\right)^2 \text{ for } \rho = \rho_{\text{nuc}} = 2 \cdot 10^{17} \text{ kg m}^{-3}$$

proton

$R = 10^{-15} \text{ m} \implies \Xi \sim 10^{-39}$   
no need for general relativity

neutron star

$R = 10^4 \text{ m} \implies \Xi \sim 0.1$   
**general relativity required !**

# Density and compactness

Spherical object of mass  $M$  and radius  $R$

- **density** :  $\rho = \frac{M}{\frac{4}{3}\pi R^3}$

- **compactness** :  $\Xi := \frac{GM}{c^2 R} \sim \frac{|E_{\text{grav}}|}{Mc^2} \sim \frac{|\Phi_{\text{surf}}|}{c^2} \sim \frac{V_{\text{esc}}^2}{c^2} \sim \frac{R_S}{R}$

$E_{\text{grav}}$  = gravitational potential energy;  $\Phi_{\text{surf}}$  = gravitational potential at the surface;  $V_{\text{esc}}$  = escape velocity from surf.;  $R_S$  = Schwarzschild radius

$$\Xi = \frac{4\pi G}{3c^2} \rho R^2 \implies \Xi = 6 \times 10^{-10} \left(\frac{R}{\text{m}}\right)^2 \text{ for } \rho = \rho_{\text{nuc}} = 2 \cdot 10^{17} \text{ kg m}^{-3}$$

proton

$$R = 10^{-15} \text{ m} \implies \Xi \sim 10^{-39}$$

no need for general relativity

neutron star

$$R = 10^4 \text{ m} \implies \Xi \sim 0.1$$

general relativity required !

*Remark:*  $\Xi_{\text{Earth}} \sim 10^{-10}$     $\Xi_{\text{Sun}} \sim 10^{-6}$     $\Xi_{\text{white dwarf}} \sim 10^{-4}$     $\Xi_{\text{black hole}} \sim 1$



# Einstein equation

$$R - \frac{1}{2}Rg = \frac{8\pi G}{c^4}T$$

- $g$  = metric tensor on the 4-dimensional spacetime manifold  $\mathcal{M}$
- $R$  = Ricci tensor ;  $R = \text{tr}_g R$
- $T$  = matter stress-energy tensor  
 perfect fluid :  $T = (e + p)u \otimes u + pg$  ( $e$  = proper energy density,  $p$  = pressure,  $u$  = fluid 4-velocity)

## Einstein equation

$$R - \frac{1}{2}Rg = \frac{8\pi G}{c^4}T$$

- $g$  = metric tensor on the 4-dimensional spacetime manifold  $\mathcal{M}$
- $R$  = Ricci tensor ;  $R = \text{tr}_g R$
- $T$  = matter stress-energy tensor  
perfect fluid :  $T = (e + p)u \otimes u + pg$  ( $e$  = proper energy density,  $p$  = pressure,  $u$  = fluid 4-velocity)

Coordinate system  $(x^\alpha)$  on  $\mathcal{M} \Rightarrow$  Einstein equation results in a system of 10 **coupled non-linear second order partial differential equations** for the 10 coefficients  $g_{\alpha\beta}$  of the metric tensor

$$R_{\alpha\beta} = -\frac{1}{2}g^{\mu\nu} \left( \frac{\partial^2 g_{\alpha\beta}}{\partial x^\mu \partial x^\nu} + \frac{\partial^2 g_{\mu\nu}}{\partial x^\alpha \partial x^\beta} - \frac{\partial^2 g_{\nu\beta}}{\partial x^\alpha \partial x^\mu} - \frac{\partial^2 g_{\alpha\nu}}{\partial x^\beta \partial x^\mu} \right) + Q_{\alpha\beta} \left( g_{\mu\nu}, \frac{\partial g_{\mu\nu}}{\partial x^\rho} \right)$$

$$R = g^{\mu\nu} R_{\mu\nu} \quad T_{\alpha\beta} = (e + p)u_\alpha u_\beta + pg_{\alpha\beta}$$

# Stationary rotating star

- **stationarity:**  $\exists$  coordinates  $(x^\alpha)$  on  $\mathcal{M}$  such that  $\frac{\partial g_{\alpha\beta}}{\partial x^0} = 0$  and  $\mathbf{k} := \frac{\partial}{\partial x^0}$  asymptotically timelike
- **axisymmetry:**  $\exists$  coordinates  $(x^\alpha)$  on  $\mathcal{M}$  such that  $\frac{\partial g_{\alpha\beta}}{\partial x^3} = 0$ ,  $\mathbf{m} := \frac{\partial}{\partial x^3}$  spacelike, vanishes on a 2-surface (*rotation axis*) and has closed orbits

$\mathbf{k}$  and  $\mathbf{m}$  are called **Killing vectors** associated with resp. stationarity and axisymmetry

Stationarity + axisymmetry  $\Rightarrow \exists$  coord.  $(x^\alpha) = (t, r, \theta, \varphi)$  on  $\mathcal{M}$  such that

$$g_{\alpha\beta} = g_{\alpha\beta}(r, \theta)$$

# Stationary rotating star

- **stationarity:**  $\exists$  coordinates  $(x^\alpha)$  on  $\mathcal{M}$  such that  $\frac{\partial g_{\alpha\beta}}{\partial x^0} = 0$  and  $\mathbf{k} := \frac{\partial}{\partial x^0}$  asymptotically timelike
- **axisymmetry:**  $\exists$  coordinates  $(x^\alpha)$  on  $\mathcal{M}$  such that  $\frac{\partial g_{\alpha\beta}}{\partial x^3} = 0$ ,  $\mathbf{m} := \frac{\partial}{\partial x^3}$  spacelike, vanishes on a 2-surface (*rotation axis*) and has closed orbits

$\mathbf{k}$  and  $\mathbf{m}$  are called **Killing vectors** associated with resp. stationarity and axisymmetry

Stationarity + axisymmetry  $\Rightarrow \exists$  coord.  $(x^\alpha) = (t, r, \theta, \varphi)$  on  $\mathcal{M}$  such that

$$g_{\alpha\beta} = g_{\alpha\beta}(r, \theta)$$

Another important simplification: **Papapetrou theorem:**

if  $\mathbf{u} = u^0 \mathbf{k} + u^\varphi \mathbf{m}$  (circular motion), then  $\exists$  coordinates  $(x^\alpha) = (t, r, \theta, \varphi)$  on  $\mathcal{M}$  such that  $g_{tr} = 0$ ,  $g_{t\theta} = 0$ ,  $g_{r\theta} = 0$ ,  $g_{r\varphi} = 0$ ,  $g_{\theta\varphi} = 0$ , i.e.

$$g_{\alpha\beta} dx^\alpha dx^\beta = -N^2 dt^2 + A^2 (dr^2 + r^2 d\theta^2) + B^2 r^2 \sin^2 \theta (d\varphi + \beta^\varphi dt)^2$$

$$N = N(r, \theta), \quad \beta^\varphi = \beta^\varphi(r, \theta), \quad A = A(r, \theta), \quad B = B(r, \theta)$$

(quasi-isotropic coordinates)

# Stationary rotating star in QI coordinates

$$g_{\alpha\beta} dx^\alpha dx^\beta = -N^2 c^2 dt^2 + A^2 (dr^2 + r^2 d\theta^2) + B^2 r^2 \sin^2 \theta (d\varphi + \beta^\varphi dt)^2$$

$$N = N(r, \theta), \quad \beta^\varphi = \beta^\varphi(r, \theta), \quad A = A(r, \theta), \quad B = B(r, \theta)$$

Important limits:

- Vanishing gravitational field :  $N \rightarrow 1$ ,  $\beta^\varphi \rightarrow 0$ ,  $A \rightarrow 1$ ,  $B \rightarrow 1$   

$$g_{\alpha\beta} dx^\alpha dx^\beta = -c^2 dt^2 + dr^2 + r^2 d\theta^2 + r^2 \sin^2 \theta d\varphi^2$$
 (Minkowski metric in spherical coordinates)

# Stationary rotating star in QI coordinates

$$g_{\alpha\beta}dx^\alpha dx^\beta = -N^2c^2dt^2 + A^2(dr^2 + r^2d\theta^2) + B^2r^2\sin^2\theta(d\varphi + \beta^\varphi dt)^2$$

$$N = N(r, \theta), \quad \beta^\varphi = \beta^\varphi(r, \theta), \quad A = A(r, \theta), \quad B = B(r, \theta)$$

Important limits:

- Vanishing gravitational field :  $N \rightarrow 1$ ,  $\beta^\varphi \rightarrow 0$ ,  $A \rightarrow 1$ ,  $B \rightarrow 1$

$$g_{\alpha\beta}dx^\alpha dx^\beta = -c^2dt^2 + dr^2 + r^2d\theta^2 + r^2\sin^2\theta d\varphi^2$$

(Minkowski metric in spherical coordinates)

- Spherical symmetry :  $\beta^\varphi \rightarrow 0$ ,  $A = B \rightarrow 0$

$$g_{\alpha\beta}dx^\alpha dx^\beta = -N^2c^2dt^2 + A^2(dr^2 + r^2d\theta^2 + r^2\sin^2\theta d\varphi^2)$$

# Stationary rotating star in QI coordinates

$$g_{\alpha\beta} dx^\alpha dx^\beta = -N^2 c^2 dt^2 + A^2 (dr^2 + r^2 d\theta^2) + B^2 r^2 \sin^2 \theta (d\varphi + \beta^\varphi dt)^2$$

$$N = N(r, \theta), \quad \beta^\varphi = \beta^\varphi(r, \theta), \quad A = A(r, \theta), \quad B = B(r, \theta)$$

Important limits:

- Vanishing gravitational field :  $N \rightarrow 1$ ,  $\beta^\varphi \rightarrow 0$ ,  $A \rightarrow 1$ ,  $B \rightarrow 1$

$$g_{\alpha\beta} dx^\alpha dx^\beta = -c^2 dt^2 + dr^2 + r^2 d\theta^2 + r^2 \sin^2 \theta d\varphi^2$$

(Minkowski metric in spherical coordinates)

- Spherical symmetry :  $\beta^\varphi \rightarrow 0$ ,  $A = B \rightarrow 0$

$$g_{\alpha\beta} dx^\alpha dx^\beta = -N^2 c^2 dt^2 + A^2 (dr^2 + r^2 d\theta^2 + r^2 \sin^2 \theta d\varphi^2)$$

- Weak gravitational field:

$$g_{\alpha\beta} dx^\alpha dx^\beta = - \left( 1 + 2 \frac{\Phi}{c^2} \right) c^2 dt^2 + \left( 1 - 2 \frac{\Phi}{c^2} \right) (dr^2 + r^2 d\theta^2 + r^2 \sin^2 \theta d\varphi^2)$$

$\Phi \sim$  Newtonian gravitational potential;  $|\Phi_{\text{surf}}|/c^2 = \Xi$  (compactness)

## Einstein equations for a stationary rotating star

In QI coord., the Einstein equations reduce to **4 elliptic equations**:

$$\Delta_3 \nu = 4\pi A^2 (E + S^i{}_i) + \frac{B^2 r^2 \sin^2 \theta}{2N^2} (\partial\beta^\varphi)^2 - \partial\nu \partial(\nu + \ln B)$$

$$\tilde{\Delta}_3 (\beta^\varphi r \sin \theta) = 16\pi \frac{NA^2}{B^2} \frac{J_\varphi}{r \sin \theta} - r \sin \theta \partial\beta^\varphi \partial(3 \ln B - \nu)$$

$$\Delta_2 [(NB - 1) r \sin \theta] = 8\pi NA^2 B (S^r{}_r + S^\theta{}_\theta) r \sin \theta$$

$$\Delta_2 \zeta = 8\pi A^2 S^\varphi{}_\varphi + \frac{3B^2 r^2 \sin^2 \theta}{4N^2} (\partial\beta^\varphi)^2 - (\partial\nu)^2$$

with the abbreviations:  $\nu := \ln N$ ,  $\zeta := \ln(AN)$

$$\Delta_2 := \frac{\partial^2}{\partial r^2} + \frac{1}{r} \frac{\partial}{\partial r} + \frac{1}{r^2} \frac{\partial^2}{\partial \theta^2} \quad \Delta_3 := \frac{\partial^2}{\partial r^2} + \frac{2}{r} \frac{\partial}{\partial r} + \frac{1}{r^2} \frac{\partial^2}{\partial \theta^2} + \frac{1}{r^2 \tan \theta} \frac{\partial}{\partial \theta}$$

$$\tilde{\Delta}_3 := \Delta_3 - \frac{1}{r^2 \sin^2 \theta} \quad \partial a \partial b := \frac{\partial a}{\partial r} \frac{\partial b}{\partial r} + \frac{1}{r^2} \frac{\partial a}{\partial \theta} \frac{\partial b}{\partial \theta}$$



# Fluid equations

Energy momentum conservation :  $\nabla \cdot T = 0$

**Circular motion** :  $u = \lambda \ell$  with  $\ell = k + \Omega m$ ,  $\Omega =$  angular rotation velocity

**Rigid rotation** :  $\Omega = \text{const} \Rightarrow \ell$  Killing vector  $\Rightarrow \exists$  a first integral to  $\nabla \cdot T = 0$ :

$$\ell \cdot (hu) = \text{const}$$

with  $h := \frac{e+p}{m_B n c^2}$  (specific enthalpy).

Newtonian limit :  $(h-1) + \Phi - \frac{1}{2}(\Omega \times r)^2 = \text{const}$

# Fluid equations

Energy momentum conservation :  $\nabla \cdot T = 0$

**Circular motion** :  $u = \lambda \ell$  with  $\ell = k + \Omega m$ ,  $\Omega =$  angular rotation velocity

**Rigid rotation** :  $\Omega = \text{const} \Rightarrow \ell$  Killing vector  $\Rightarrow \exists$  a first integral to  $\nabla \cdot T = 0$ :

$$\ell \cdot (hu) = \text{const}$$

with  $h := \frac{e+p}{m_B n c^2}$  (specific enthalpy).

Newtonian limit :  $(h-1) + \Phi - \frac{1}{2}(\Omega \times r)^2 = \text{const}$

**Equation of state (EOS)**: cold dense matter:  $e = e(h)$ ,  $p = p(h)$ ,  $n = n(h)$

# Fluid equations

Energy momentum conservation :  $\nabla \cdot T = 0$

**Circular motion** :  $u = \lambda \ell$  with  $\ell = k + \Omega m$ ,  $\Omega =$  angular rotation velocity

**Rigid rotation** :  $\Omega = \text{const} \Rightarrow \ell$  Killing vector  $\Rightarrow \exists$  a first integral to  $\nabla \cdot T = 0$ :

$$\ell \cdot (hu) = \text{const}$$

with  $h := \frac{e+p}{m_B n c^2}$  (specific enthalpy).

Newtonian limit :  $(h-1) + \Phi - \frac{1}{2}(\Omega \times r)^2 = \text{const}$

**Equation of state (EOS)**: cold dense matter:  $e = e(h)$ ,  $p = p(h)$ ,  $n = n(h)$

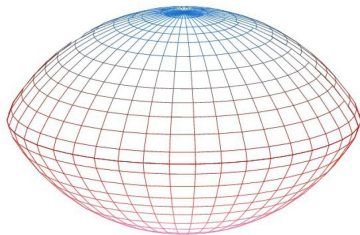
closed system of equations

At fixed EOS, a model is fully specified by two parameters, e.g. central density and  $\Omega$ .

# Computational code

Framework: **RotStar** code based on LORENE C++ library

<http://www.lorene.obspm.fr/>



Resolution of Einstein equations for stationary axisymmetric rotating stars

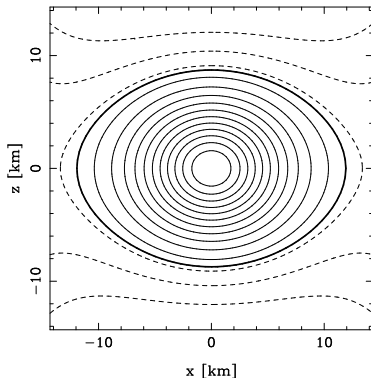
*Numerical technique: spectral methods*  
⇒ high accuracy

*Microphysics input: equation of state (EOS)*

# Examples of numerical results

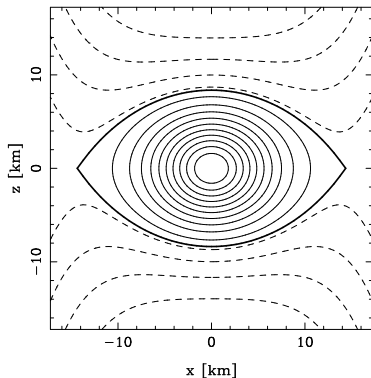
## Rapidly rotating model

Enthalpy isocontours ( $f=1$  kHz)



## Maximum rotation rate (Keplerian limit)

Enthalpy isocontours Keplerian frequency



Isocontour of specific enthalpy  $h$  :

$h < 1 \iff$  stellar exterior (dashed lines);  $h = 1 \iff$  stellar surface (thick solid line)

$h > 1 \iff$  stellar interior (solid line)

# Global quantities

- $M$  : gravitational mass (\*)
- $M_B$  : baryon mass =  $m_B \times$  total baryon number
- $J$  : total angular momentum (about the rotation axis) (\*)
- $\Omega$  : angular rotation frequency (as seen from infinity)
- $R$  : circumferential radius of the equator
- $z_p, z_{eq}^{\pm}$  : redshifts from pole, and equator (forward and backward) (\*)
- $f_{ISCO}$  : orbital frequency at the innermost stable circular orbit (\*)

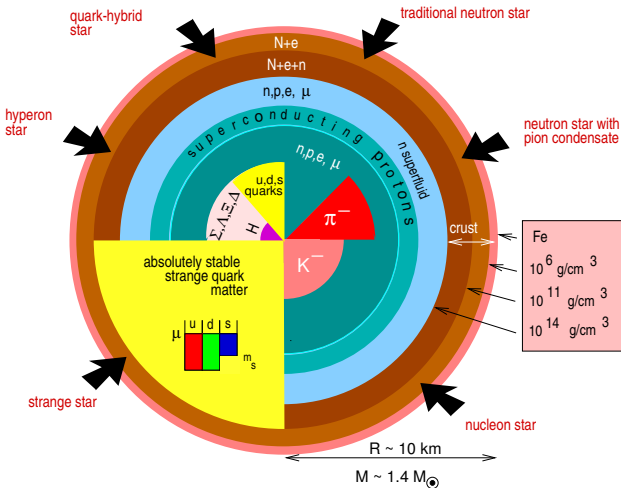
(\*) = measurable quantities

# Outline

- 1 Compact stars in general relativity
- 2 Confronting theoretical models and observations: astrophysics as a lab**
- 3 The search for strange stars
- 4 Gravitational wave observations

# Our (poor) knowledge of matter at supernuclear densities

## Internal structure of compact stars

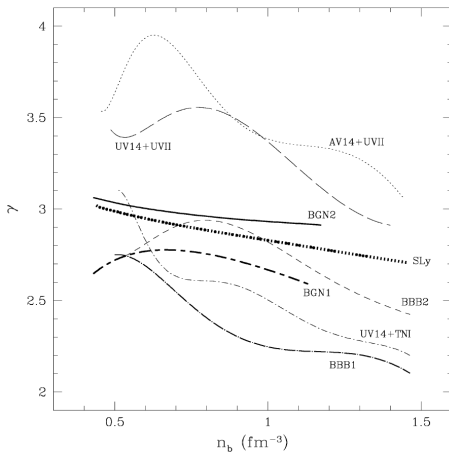


[Weber, J. Phys. G 27, 465 (2001)]

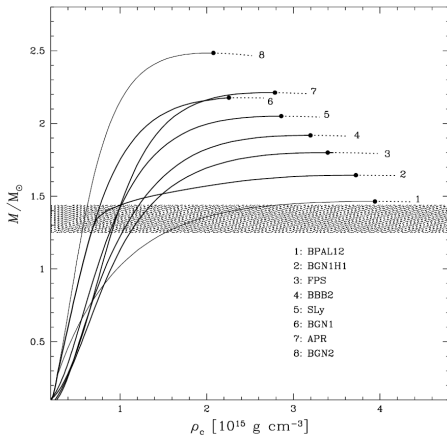


## Large discrepancies in theoretical models...

adiabatic index



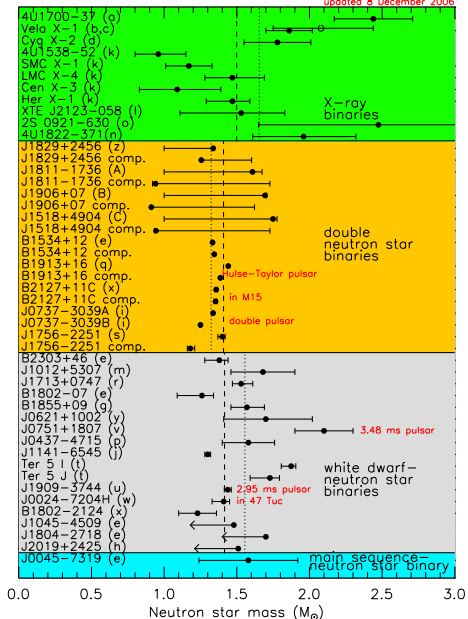
non-rotating neutron star mass



[Haensel, Potekhin &amp; Yakovlev (2007)]

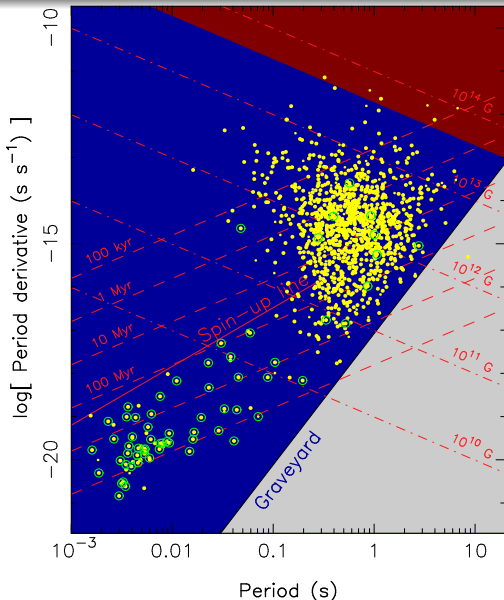
# Measured neutron star masses

updated 8 December 2006



[Lattimer & Prakash, astro-ph/0612440 (2006)]

# Measured rotation velocity



← Period derivative  $\dot{P}$  vs period  $P$   
for radio pulsars

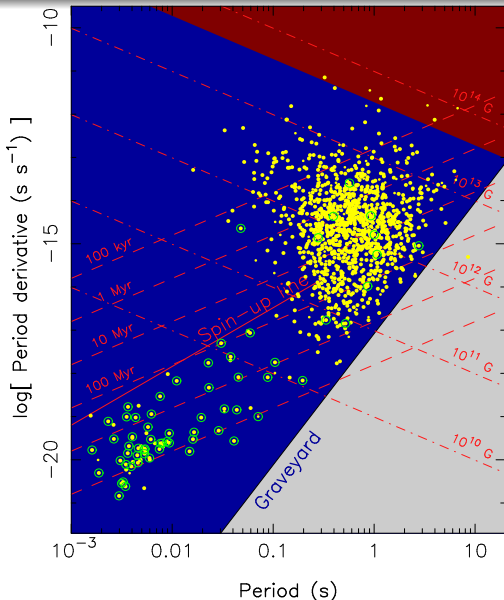
[Lorimer, *Liv. Rev. Relat.* **8**, 7 (2005)]

Fastest pulsar known to date:  
PSR J1748-2446ad

$P = 1.396$  ms    $f = 716$  Hz

[Hessels et al., *Science* **311**, 1901 (2006)]

# Measured rotation velocity



← Period derivative  $\dot{P}$  vs period  $P$   
for radio pulsars

[Lorimer, *Liv. Rev. Relat.* **8**, 7 (2005)]

Fastest pulsar known to date:  
PSR J1748-2446ad

$P = 1.396$  ms    $f = 716$  Hz

[Hessels et al., *Science* **311**, 1901 (2006)]

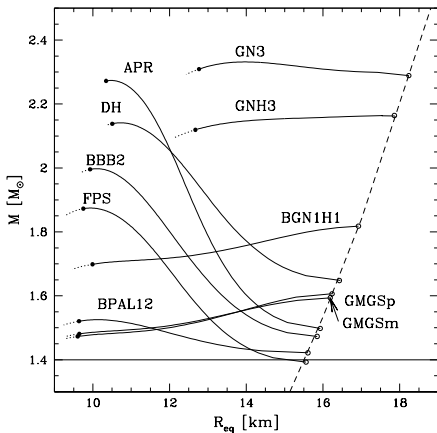
Discovery of an oscillation frequency  
of  $f = 1122$  Hz in a X-ray burst  
from X-ray transient XTE J1739-285

[Kaaret et al., *ApJL* **657**, 97 (2007)]

Spin frequency ? This would imply  
 $P = 0.89$  ms !

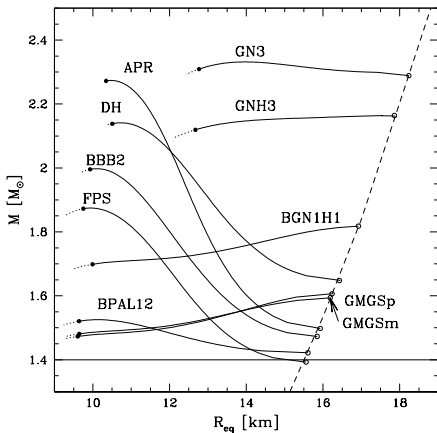
*Not confirmed yet !*

## Impact of the discovery of very high rotation frequencies

Mass-radius relation at  $f = 1122$  Hz[Bejger, Haensel & Zdunik, *A&A* **464**, L49 (2007)]

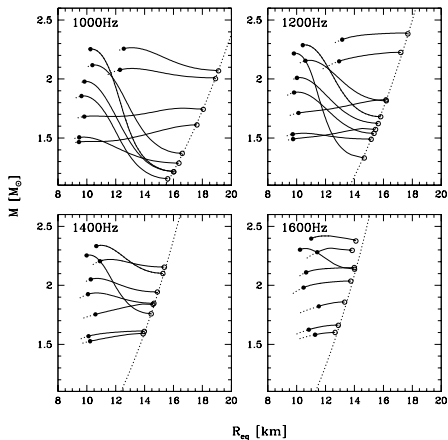
# Impact of the discovery of very high rotation frequencies

## Mass-radius relation at $f = 1122$ Hz



[Bejger, Haensel & Zdunik, *A&A* **464**, L49 (2007)]

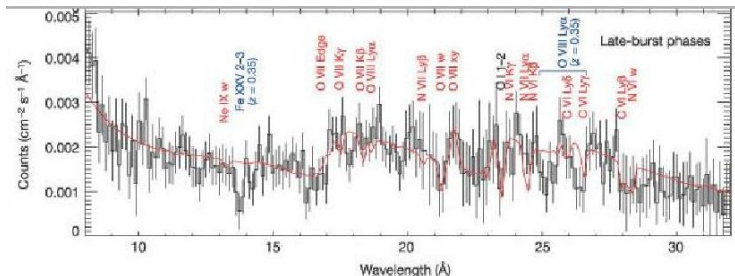
## Mass-radius relation at fixed $f$



[Zdunik, Haensel, Bejger & Gourgoulhon,  
arXiv:0710.5010]

# Measured compactness ( $M/R$ )

Observation (XMM-Newton) of iron and oxygen spectral lines from the compact star in the low-mass X-ray binary EXO 07748-676



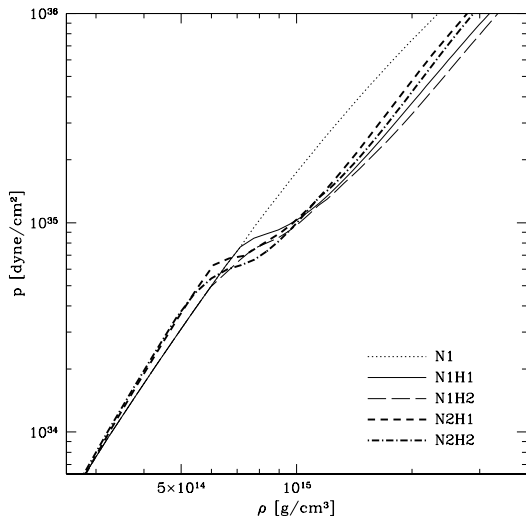
[Cottam, Paerels & Mendez, *Nature* **420**, 51 (2002)]

⇒ **gravitational redshift**:  $z = \frac{\lambda_{\text{obs}} - \lambda}{\lambda} = 0.35$  (NB:  $z_{\text{Doppler}} \sim 10^{-3}$ )

$$z = (1 - 2\Xi)^{-1/2} - 1 = 0.35 \implies \Xi = \frac{GM}{c^2 R} = 0.23$$

Unfortunately we know neither  $M$  nor  $R$  for this system...

## Search for an indicator of hyperonization of matter (1/2)



Hyperon = baryon (i.e. hadron + fermion) made of 3 quarks, with at least one **strange quark**:

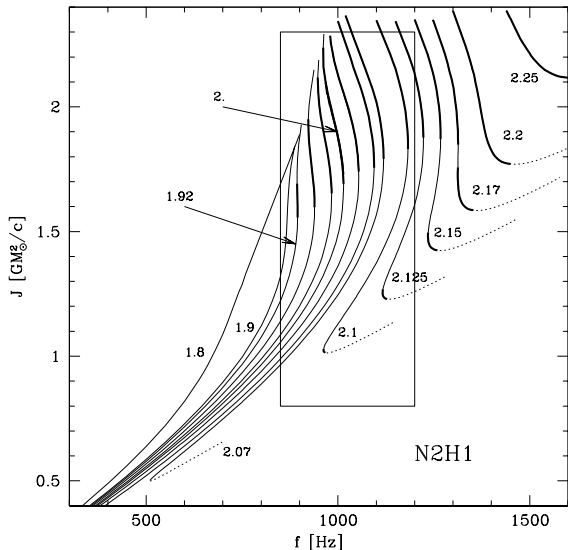
- $\Lambda_0 = uds$
- $\Sigma^- = dds$
- $\Xi^0 = uss$
- etc...

Should appear at high density ( $\rho > 2\rho_{\text{nuc}}$ )  
 $\Rightarrow$  **EOS softening**

$N1 = np$ ,  $N1H1, N2H1 = np\Lambda\Sigma$ ,  
 $N1H2, N2H2 = np\Lambda\Sigma\Xi$   
 Balberg & Gal (1997)



## Search for an indicator of hyperonization of matter (2/2)



Hyperon softening of the EOS  $\Rightarrow$  **back-bending** :  
 spin-up by angular momentum **loss**

Detectability: pulsar with  $\dot{P} < 0$

[Zdunik, Haensel, Gourgoulhon & Bejger, A&A 416, 1013 (2004)]

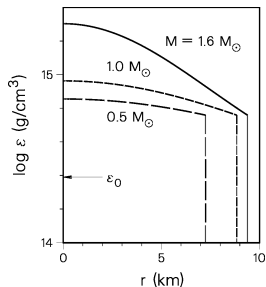
# Outline

- 1 Compact stars in general relativity
- 2 Confronting theoretical models and observations: astrophysics as a lab
- 3 The search for strange stars**
- 4 Gravitational wave observations

# A short history of strange stars

- **1970:** N. Itoh considered compact stars made of free degenerate Fermi gas of  $u$ ,  $d$  and  $s$  quarks of equal mass  $m_q = 10 \text{ GeV}/c^2$  (not self-bound, vanishing density at the surface)  $\Rightarrow M_{\text{max}} = 10^{-3} M_{\odot}$ .
- **1971:** A.R. Bodmer: the ground state of nuclear matter may be a state of **deconfined quarks**.
- **1984:** E. Witten reformulated (independently) this idea, and contemplated the possibility that neutron stars are in fact **strange quark stars**.
- **1986:** first detailed numerical models of static strange stars by P. Haensel, J.L. Zdunik & R. Schaeffer, as well as C. Alcock, E. Farhi & A.V. Olinto.
- **1989:** announcement of a half-millisecond pulsar in SN 1987A
- **1996:** discovery of high frequency QPO in low-mass X-ray binaries
- **2002:** NASA announcement of “discovery” of two strange stars

# Basic properties of strange stars

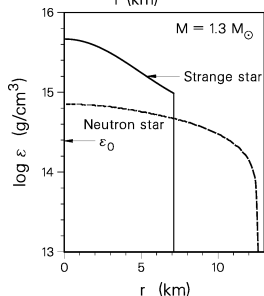


Simplest models: improved **MIT bag model**

⇒ 3-parameter EOS for SQM matter:

$B$ : bag constant,  $m_s$  mass of  $s$  quark,  $\alpha_s$ : QCD structure constant ( $\alpha_s = g^2/(4\pi)$ ,  $g$ : QCD coupling constant)

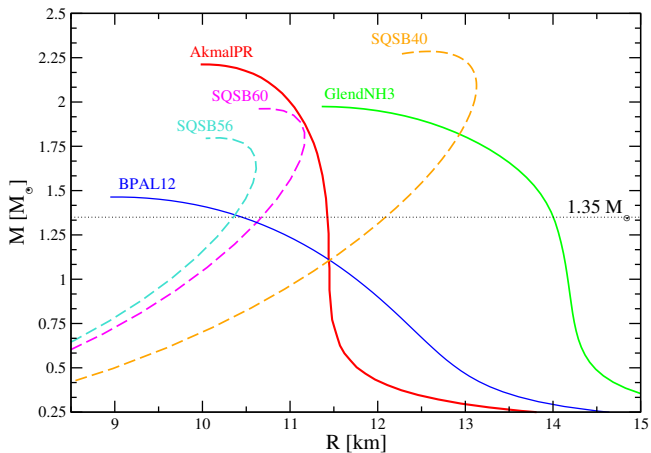
- finite density at the surface (zero pressure)
- for small mass (weak gravity): almost constant density profile  $\epsilon \sim 4B$
- more compact than neutron stars



← figures from [Glendenning (1997)]

# Mass-radius relation

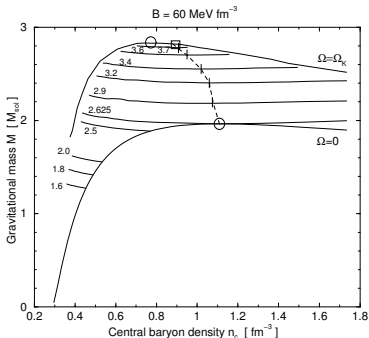
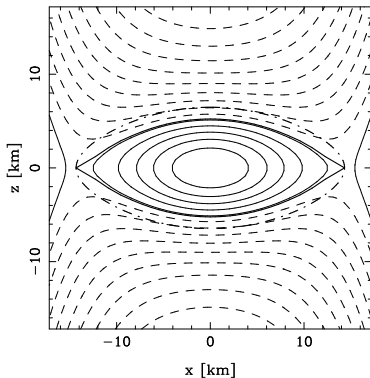
## From strangelets to strange stars



[Gondek-Rosińska, Bejger, Bulik, Gourgoulhon, Haensel, Limousin, Taniguchi & Zdunik, *ASR* **39**, 271 (2007)]

## Rapidly rotating strange stars

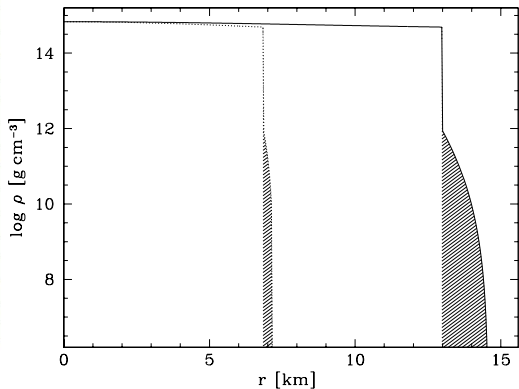
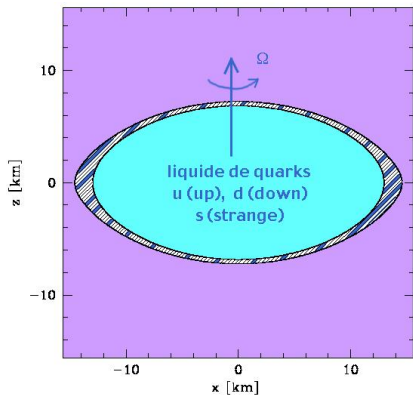
Enthalpy



[Gourgoulhon, Haensel, Livine, Paluch, Bonazzola & Marck, *A&A* **349**, 851 (1999)]

Minimal rotation period (for  $m_s = 0$  and  $\alpha_s = 0$ ):  $P_{\min} = 0.634 B_{60}^{-1/2}$  ms

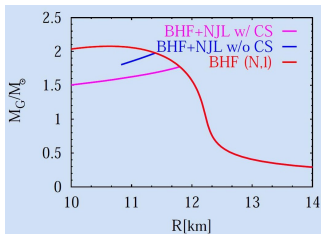
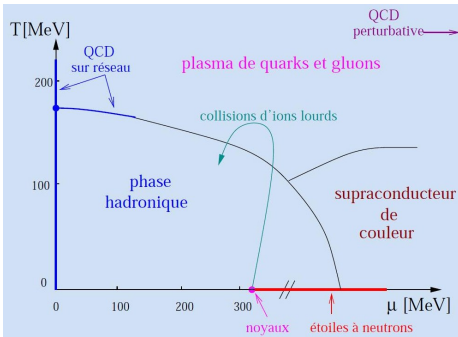
# Models with solid crust



EOS:  $B = 56 \text{ MeV fm}^{-3}$ ,  $\alpha_s = 0.2$ ,  $m_s = 200 \text{ MeV } c^{-2}$   
 star:  $M_B = 1.63 M_\odot$ ,  $f = 1210 \text{ Hz}$ .

[Zdunik, Haensel, Gourgoulhon, A&A 372, 535 (2001)]

# Recent studies of quark matter



- Study of quark matter ( $u, d, s$ ) in color-flavor-locked (CFL) states  $\Rightarrow$  No stable configuration with uniquely CFL matter

[Buballa, Neumann, Oertel & Shovkoy, PLB **595**, 36 (2004)]

- Goldstone bosons in CFL states

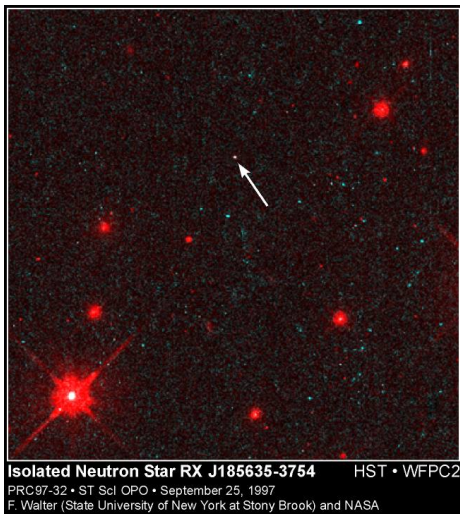
[Werth, Buballa & Oertel, PPNP **59**, 308 (2007)], [Kleinhaus, Buballa, Nickel & Oertel, PRD **76**, 074024 (2007)]

- Color superconductivity effects on the properties of a strange star: electron atmosphere, transport properties

[Oertel & Urban, PRD **77**, 074015 (2008)]



# The case of RX J1856.5-3754



- Discovered as an X-ray source with ROSAT in 1996 [Walter et al., *Nature* **379**, 233 (1996)]

Best fit black body  $kT_{\infty} = 57 \pm 1$  eV

$$\iff T_{\infty} \simeq 6.6 \times 10^5 \text{ K}$$

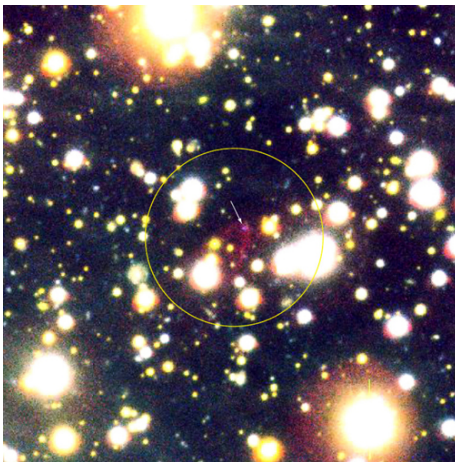
In front of molecular cloud *R Coronae Australis*  $\Rightarrow d \lesssim 130 - 170$  pc

- Optical counterpart discovered in 1997 with HST [Walter & Matthews, *Nature* **389**, 358 (1997)]

magnitude  $V = 25.6$

Optical flux 2 to 3 times larger than the tail of the 57 eV black body

## RX J1856.5-3754 observed by VLT

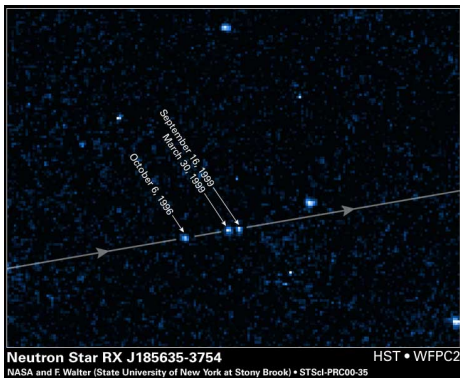


VLT Kueyen + FORS2 (field:  $80'' \times 80''$ )

→ bowshock (heated interstellar gas by accelerated  $e^-$  and  $p$  from the star ?)

[ESO 2000]

## Distance to RX J1856.5-3754

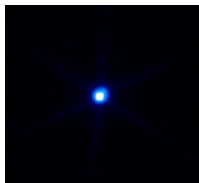


- First measure of proper motion and parallax (erroneous) [Walter, ApJ 549, 433 (2001)]

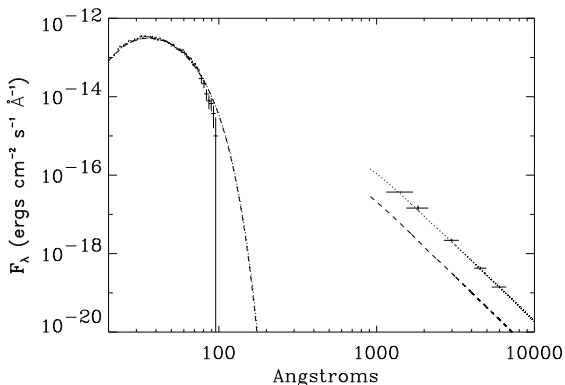
⇒ erroneous  $d = 61 \pm 9$  pc

- Correct determinations of parallax:  
 $d = 140 \pm 40$  pc [Kaplan, van Kerkwijk, Anderson, ApJ 571, 447 (2002)]  
 $d = 117 \pm 12$  pc [Walter & Lattimer, ApJ 576, L145 (2002)]

## RX J1856.5-3754 spectrum



Chandra image of RX  
J1856.5-3754



Spectrum from Chandra, EUVE and HST data:

- - - - : black body best fit to Chandra data  $kT_{\infty} = 63 \text{ eV}$

[Burwitz et al., *A&A* **379**, L35 (2001)]

.....:  $63 \text{ eV}$  black body +  $15 \text{ eV}$  black body with  $R_{\infty}(15 \text{ eV}) = 5R_{\infty}(63 \text{ eV})$

[Walter & Lattimer, *ApJ* **576**, L145 (2002)]

## Is RX J1856.5-3754 a strange star ?

The small “radius” issue:

Assuming black body emission from the **entire** surface :

$$R_{\infty} = \frac{d}{T_{\infty}^2} \left( \frac{f_{\infty}}{\sigma} \right)^{1/2}$$

$$R_{\infty} = \left( 1 - \frac{2GM}{c^2 R} \right)^{-1/2} R > R$$

- Distance of Walter & Lattimer 2002 :  $d = 117 \text{ pc} \Rightarrow R_{\infty} = 4.8 \text{ km}$
- Distance of Kaplan et al. 2002 :  $d = 140 \text{ pc} \Rightarrow R_{\infty} = 5.8 \text{ km}$

## Is RX J1856.5-3754 a strange star ?

The small “radius” issue:

Assuming black body emission from the **entire** surface :

$$R_{\infty} = \frac{d}{T_{\infty}^2} \left( \frac{f_{\infty}}{\sigma} \right)^{1/2}$$

$$R_{\infty} = \left( 1 - \frac{2GM}{c^2 R} \right)^{-1/2} R > R$$

- Distance of Walter & Lattimer 2002 :  $d = 117 \text{ pc} \Rightarrow R_{\infty} = 4.8 \text{ km}$
- Distance of Kaplan et al. 2002 :  $d = 140 \text{ pc} \Rightarrow R_{\infty} = 5.8 \text{ km}$

Recent discovery of pulsations of period  $P = 7.055 \text{ s}$  from XMM-Newton observations (with a pulsed fraction of only 1.2%)

[Tiengo & Mereghetti, ApJ **657**, L101 (2007)]

$\Rightarrow$  Hot spot model favored today

# Outline

- 1 Compact stars in general relativity
- 2 Confronting theoretical models and observations: astrophysics as a lab
- 3 The search for strange stars
- 4 Gravitational wave observations**

# Observing compact stars via gravitational waves

LIGO: USA, Louisiana



LIGO: USA, Washington



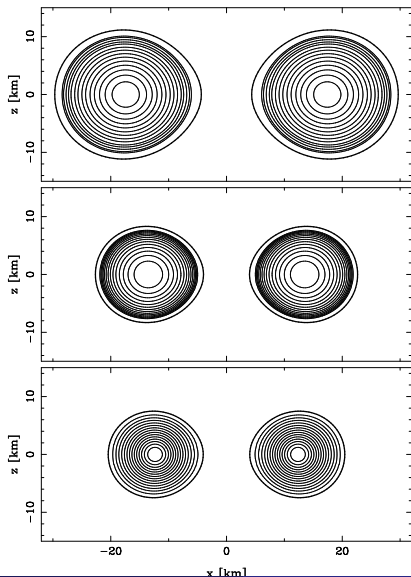
VIRGO: France/Italy (Pisa)



Michelson-type lasers  
 VIRGO (3 km) and LIGO  
 (4 km)  $\Rightarrow$  they are  
 currently acquiring data.



# Constraints on EOS from gravitational radiation (1/2)



GW from inspiraling binary  
neutrons stars

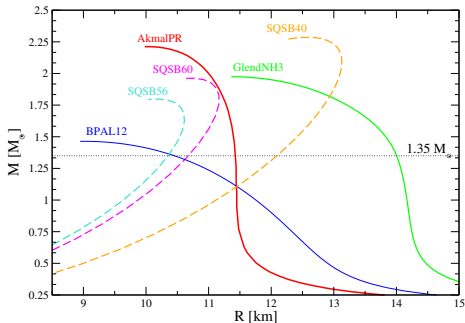
Primary target for VIRGO /  
LIGO

← Irrotational binary  
configurations close to  
mass-shedding limit for  
GlendNH3, AkmalPR and  
BPAL12 EOS

[Bejger, Gondek-Rosińska, Gourgoulhon,  
Haensel, Taniguchi & Zduńik, *A&A* 431,  
297 (2005)]

# Constraints on EOS from gravitational radiation (2/2)

3 nuclear matter EOS  
3 strange matter EOS



[Bejger, Gondek-Rosińska, Gourgoulhon, Haensel, Taniguchi & Zdunik, *A&A* **431**, 297 (2005)]

[Limousin, Gondek-Rosińska & Gourgoulhon, *PRD* **71**, 064012 (2005)]

[Gondek-Rosińska, Bejger, Bulik, Gourgoulhon, Haensel, Limousin, Taniguchi & Zdunik, *ASR* **39**, 271 (2007)]

Inspiring sequences

